

 $K\omega$ Documentation Release 2.0.0

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CHAPTER 1

Overview

This document is a manual for $K\omega$ which is the library to solve the shifted linear equation within the Krylov subspace. This library provides routines to solve the following shifted linear equation (with the projection),

$$G_{ij}(z) = \langle i|(z\hat{I} - \hat{H})^{-1}|j\rangle \equiv \varphi_i^* \cdot (z\hat{I} - \hat{H})^{-1}\varphi_j.$$
(1.1)

The source codes of $K\omega$ is written in FORTRAN and requires the BLAS Level 1 routines.

Algorithm

This library provides the four kinds of numerical solvers. The kind of solvers is selected under the condition whether the Hamiltonian \hat{H} and/or the frequency z are complex or real number. It is noted that \hat{H} must be Hermitian (symmetric) for complex (real) number.

- (\hat{H}, z) = (complex, complex): Shifted Bi-Conjugate Gradient(BiCG) method [1]
- (\hat{H}, z) = (real, complex): Shifted Conjugate Orthogonal Conjugate Gradient(COCG) method [2]
- (\hat{H}, z) = (complex, real): Shifted Conjugate Gradient(CG) method (using complex vector)
- (\hat{H}, z) = (real, real): Shifted Conjugate Gradient(CG) method (using real vector)

For above methods, seed switching [2] is adopted. Hereafter, the number of the left (right) side vector is written as N_L (N_R). The details of each algorithm are written as follows.

2.1 Shifted BiCG method with seed switching technique

$$\begin{split} G_{ij}(z_k) &= 0 (i = 1 \cdots N_L, \ j = 1 \cdots N_R, \ k = 1 \cdots N_z) \\ \text{do } j &= 1 \cdots N_R \\ \boldsymbol{r} &= \boldsymbol{\varphi}_j, \\ \tilde{\boldsymbol{r}} &= \text{an arbitrary vector, } \boldsymbol{r}^{\text{old}} &= \tilde{\boldsymbol{r}}^{\text{old}} = \boldsymbol{0} \\ p_{ik} &= 0 (i = 1 \cdots N_L, \ k = 1 \cdots N_z), \ \pi_k = \pi_k^{\text{old}} = 1 (k = 1 \cdots N_z) \\ \rho &= \infty, \ \alpha = 1, \ z_{\text{seed}} = 0 \\ \text{do iteration} \\ &\circ \text{Seed equation} \\ &\circ \text{Seed equation} \\ \rho^{\text{old}} &= \rho, \ \rho = \tilde{\boldsymbol{r}}^* \cdot \boldsymbol{r} \\ \beta &= \rho/\rho^{\text{old}} \\ \boldsymbol{q} &= (z_{\text{seed}} \hat{\boldsymbol{I}} - \hat{\boldsymbol{H}}) \boldsymbol{r} \\ \alpha^{\text{old}} &= \alpha, \ \alpha = \frac{\rho}{\tilde{\boldsymbol{r}}^* \cdot \boldsymbol{q} - \beta \rho/\alpha} \\ &\circ \text{Shifted equation} \\ \text{do } k &= 1 \cdots N_z \end{split}$$

$$\begin{split} \pi_k^{\text{new}} &= [1 + \alpha(z_k - z_{\text{seed}})] \pi_k - \frac{\alpha\beta}{\alpha^{\text{old}}} (\pi_k^{\text{old}} - \pi_k) \\ &\text{do } i = 1 \cdots N_L \\ p_{ik} &= \frac{1}{\pi_k} \boldsymbol{\varphi}_i^* \cdot \boldsymbol{r} + \frac{\pi_k^{\text{old}} \pi_k^{\text{old}}}{\pi_k \pi_k} \beta p_{ik} \\ G_{ij}(z_k) &= G_{ij}(z_k) + \frac{\pi_k}{\pi_k^{\text{new}}} \alpha p_{ik} \\ \pi_k^{\text{old}} &= \pi_k, \pi_k = \pi_k^{\text{new}} \\ &\text{end do } i \\ &\text{end do } k \\ \boldsymbol{q} &= \left(1 + \frac{\alpha\beta}{\alpha^{\text{old}}}\right) \boldsymbol{r} - \alpha \boldsymbol{q} - \frac{\alpha\beta}{\alpha^{\text{old}}} \boldsymbol{r}^{\text{old}}, \ \boldsymbol{r}^{\text{old}} = \boldsymbol{r}, \ \boldsymbol{r} = \boldsymbol{q} \\ \boldsymbol{q} &= (z_{\text{seed}}^* \hat{\boldsymbol{I}} - \hat{\boldsymbol{H}}) \tilde{\boldsymbol{r}}, \ \boldsymbol{q} &= \left(1 + \frac{\alpha^*\beta^*}{\alpha^{\text{old}*}}\right) \tilde{\boldsymbol{r}} - \alpha^* \boldsymbol{q} - \frac{\alpha^*\beta^*}{\alpha^{\text{old}*}} \tilde{\boldsymbol{r}}^{\text{old}}, \ \tilde{\boldsymbol{r}}^{\text{old}} = \tilde{\boldsymbol{r}}, \ \tilde{\boldsymbol{r}} = \boldsymbol{q} \\ &\circ \text{Seed switch} \\ &\text{Search } k \text{ which gives the smallest } |\pi_k| \cdot \rightarrow z_{\text{seed}}, \ \pi_{\text{seed}}, \ \pi_{\text{seed}}^{\text{old}} \\ &\boldsymbol{r} &= \boldsymbol{r}/\pi_{\text{seed}}, \ \boldsymbol{r}^{\text{old}} = \boldsymbol{r}^{\text{old}}/\pi_{\text{seed}}^{\text{old}}, \ \tilde{\boldsymbol{r}} = \tilde{\boldsymbol{r}}/\pi_{\text{seed}}^*, \ \tilde{\boldsymbol{r}}^{\text{old}} = \tilde{\boldsymbol{r}}^{\text{old}}/\pi_{\text{seed}}^{\text{old}*} \\ &\alpha &= (\pi_{\text{seed}}^{\text{old}}/\pi_{\text{seed}}) \alpha, \rho = \rho/(\pi_{\text{seed}}^{\text{old}}\pi_{\text{seed}}^{\text{old}}) \\ &\{\pi_k = \pi_k/\pi_{\text{seed}}, \ \pi_k^{\text{old}} = \pi_k^{\text{old}}/\pi_{\text{seed}}^{\text{old}}\} \\ &\text{if } (|\boldsymbol{r}| < \text{Threshold}) \text{ exit} \end{aligned}$$
 end do iteration

2.2 Shifted COCG method with seed switching technique

This method is obtained by $\tilde{\boldsymbol{r}} = \boldsymbol{r}^*$, $\tilde{\boldsymbol{r}}^{\mathrm{old}} = \boldsymbol{r}^{\mathrm{old}*}$ in the BiCG method. $G_{ij}(z_k) = 0 (i = 1 \cdots N_L, \ j = 1 \cdots N_R, \ k = 1 \cdots N_z)$ do $j = 1 \cdots N_R$ $\boldsymbol{r} = \boldsymbol{\varphi}_j, \boldsymbol{r}^{\mathrm{old}} = \boldsymbol{0}$ $p_{ik} = 0 (i = 1 \cdots N_L, \ k = 1 \cdots N_z), \ \pi_k = \pi_k^{\mathrm{old}} = 1 (k = 1 \cdots N_z)$ $\rho = \infty, \ \alpha = 1, \ z_{\mathrm{seed}} = 0$ do iteration $\circ \text{ Seed equation }$ $\rho^{\mathrm{old}} = \rho, \ \rho = \boldsymbol{r} \cdot \boldsymbol{r}$ $\beta = \rho/\rho^{\mathrm{old}}$ $\boldsymbol{q} = (z_{\mathrm{seed}} \hat{\boldsymbol{I}} - \hat{\boldsymbol{H}}) \boldsymbol{r}$ $\alpha^{\mathrm{old}} = \alpha, \ \alpha = \frac{\rho}{\boldsymbol{r} \cdot \boldsymbol{q} - \beta \rho/\alpha}$ $\circ \text{ Shifted equation }$ do $k = 1 \cdots N_z$

end do j

$$\pi_k^{\text{new}} = [1 + \alpha(z_k - z_{\text{seed}})] \pi_k - \frac{\alpha\beta}{\alpha^{\text{old}}} (\pi_k^{\text{old}} - \pi_k)$$
 do $i = 1 \cdots N_L$
$$p_{ik} = \frac{1}{\pi_k} \boldsymbol{\varphi}_i^* \cdot \boldsymbol{r} + \frac{\pi_k^{\text{old}} \pi_k^{\text{old}}}{\pi_k \pi_k} \beta p_{ik}$$

$$G_{ij}(z_k) = G_{ij}(z_k) + \frac{\pi_k}{\pi_k^{\text{new}}} \alpha p_{ik}$$

$$\pi_k^{\text{old}} = \pi_k, \, \pi_k = \pi_k^{\text{new}}$$
 end do i end do k
$$\boldsymbol{q} = \left(1 + \frac{\alpha\beta}{\alpha^{\text{old}}}\right) \boldsymbol{r} - \alpha \boldsymbol{q} - \frac{\alpha\beta}{\alpha^{\text{old}}} \boldsymbol{r}^{\text{old}}, \, \boldsymbol{r}^{\text{old}} = \boldsymbol{r}, \, \boldsymbol{r} = \boldsymbol{q}$$
 \circ Seed switch Search k which gives the smallest $|\pi_k| \cdot \rightarrow z_{\text{seed}}, \, \pi_{\text{seed}}, \, \pi_{\text{seed}}$
$$\boldsymbol{r} = \boldsymbol{r}/\pi_{\text{seed}}, \, \boldsymbol{r}^{\text{old}} = \boldsymbol{r}^{\text{old}}/\pi_{\text{seed}}^{\text{old}}$$

$$\alpha = (\pi_{\text{seed}}^{\text{old}}/\pi_{\text{seed}}) \alpha, \, \rho = \rho/(\pi_{\text{seed}}^{\text{old}}\pi_{\text{seed}}^{\text{old}})$$

$$\{\pi_k = \pi_k/\pi_{\text{seed}}, \, \pi_k^{\text{old}} = \pi_k^{\text{old}}/\pi_{\text{seed}}^{\text{old}}\}$$
 if $(|\boldsymbol{r}| < \text{Threshold})$ exit end do iteration

2.3 Shifted CG method with seed switching technique

```
This method is obtained by \tilde{r} = r, \tilde{r}^{\text{old}} = r^{\text{old}} in the BiCG method.
G_{ij}(z_k) = 0 (i = 1 \cdots N_L, \ j = 1 \cdots N_R, \ k = 1 \cdots N_z)
do j = 1 \cdots N_R
           r = \boldsymbol{arphi}_i, r^{	ext{old}} = \mathbf{0}
          p_{ik} = 0 (i = 1 \cdots N_L, \ k = 1 \cdots N_z), \ \pi_k = \pi_k^{\text{old}} = 1 (k = 1 \cdots N_z)
           \rho = \infty, \alpha = 1, z_{\text{seed}} = 0
           do iteration
                      o Seed equation

\rho^{\text{old}} = \rho, \ \rho = \boldsymbol{r}^* \cdot \boldsymbol{r}

                      \beta = \rho/\rho^{\text{old}}
                      \mathbf{q} = (z_{\text{seed}}\hat{I} - \hat{H})\mathbf{r}
                     \alpha^{\text{old}} = \alpha, \ \alpha = \frac{\rho}{r^* \cdot q - \beta \rho / \alpha}
                      o Shifted equation
                      do k = 1 \cdots N_z
                              \pi_k^{\text{new}} = [1 + \alpha(z_k - z_{\text{seed}})]\pi_k - \frac{\alpha\beta}{\alpha^{\text{old}}}(\pi_k^{\text{old}} - \pi_k)
                              do i = 1 \cdots N_L
```

end do j

$$p_{ik} = \frac{1}{\pi_k} \boldsymbol{\varphi}_i^* \cdot \boldsymbol{r} + \left(\frac{\pi_k^{\text{old}}}{\pi_k}\right)^2 \beta p_{ik}$$
$$G_{ij}(z_k) = G_{ij}(z_k) + \frac{\pi_k}{\pi_k^{\text{new}}} \alpha p_{ik}$$
$$\pi_k^{\text{old}} = \pi_k, \pi_k = \pi_k^{\text{new}}$$

end do i

 $\mathrm{end}\;\mathrm{do}\;k$

$$m{q} = \left(1 + rac{lphaeta}{lpha^{
m old}}
ight)m{r} - lpham{q} - rac{lphaeta}{lpha^{
m old}}m{r}^{
m old}, \ m{r}^{
m old} = m{r}, \ m{r} = m{q}$$

o Seed switch

Search k which gives the minimum value of $|\pi_k|$. $\to z_{\rm seed}, \; \pi_{\rm seed}, \; \pi_{\rm seed}$

$$\begin{split} & \boldsymbol{r} = \boldsymbol{r}/\pi_{\rm seed}, \ \boldsymbol{r}^{\rm old} = \boldsymbol{r}^{\rm old}/\pi_{\rm seed}^{\rm old} \\ & \alpha = (\pi_{\rm seed}^{\rm old}/\pi_{\rm seed})\alpha, \rho = \rho/\pi_{\rm seed}^{\rm old}^{2} \\ & \{\pi_{k} = \pi_{k}/\pi_{\rm seed}, \ \pi_{k}^{\rm old} = \pi_{k}^{\rm old}/\pi_{\rm seed}^{\rm old} \} \\ & \text{if}(\ |\boldsymbol{r}| < \text{Threshold}) \text{ exit} \end{split}$$

end do iteration

end do j

Schematic workflow of this library

In the following description, the loop for N_R is omitted for simplicity and instead of $G_{ij}(z_k)$, the N_L -dimensional vector \mathbf{x}_k is obtained by using the library.

The names of the routines is defined as follows.

- komega_bicg_init, komega_cocg_init, komega_cg_c_init, komega_cg_r_init

 Set the initial conditions such as the allocation of variables used in the library.
- komega_bicg_update, komega_cocg_update, komega_cg_c_update, komega_cg_r_update

These routines are called in the iteration to update the solution vectors.

• komega_bicg_finalize, komega_cocg_finalize, komega_cg_c_finalize, komega_cg_r_finalize

Release the allocated vectors in the library.

komega_bicg_getcoef, komega_cg_getcoef, komega_cg_r_getcoef

Get the α , β , z_{seed} , \mathbf{r}^{L} conserved at each iteration.

• komega_bicg_getvec, komega_cocg_getvec, komega_cg_c_getvec, komega_cg_r_getvec

Get the vectors r, r^{old} , \tilde{r} , \tilde{r}^{old} .

• komega_bicg_restart, komega_cocg_restart, komega_cg_c_restart, CG_R_restart

Note:

- Give the vector size N_H corresponding to the size of the Hilbert space and the number of the frequency z.
- Allocate the two vectors (in the case of BiCG method, four vectors) with the size of N_H .
- Give the function for the Hamiltonian-vector production.
- Allocate the solution vectors. It is noted that the length of each solution vector is not always equal to N_H . In fact, the its length in the previous section is N_L . In this case, the length of the (bi-)conjugate gradient vector $\mathbf{p}_k(k=1,\cdots N_z)$ also becomes N_L . We have to prepare a code for projecting N_H -dimensional vector onto N_L dimensional space.

$$\mathbf{r}^{\mathrm{L}}=\hat{P}^{\dagger}oldsymbol{r},\qquad \hat{P}\equiv(oldsymbol{arphi}_{1},\cdots,oldsymbol{arphi}_{N_{L}})$$

• If the result converges (or a breakdown occurs), komega_*_update return the first element of status as a negative integer. Therefore, please exit loop when status (1) < 0.

- The 2-norm is used for the convergence check in the routine komega_*_update. Therefore, if 2-norms of residual vectors at all shift points becomes smaller than threshold, this routine assumes the result is converged.
- We can obtain the history of $\alpha, \beta, \mathbf{r}^{\mathbf{L}}$ for restarting calculation. In this case, itermax must not be 0.

3.1 The schematic workflow of shifted BiCG library

Allocate
$$v_{12}, v_{13}, v_2, v_3, \{x_k\}, \mathbf{r}^L v_2 = \varphi_j$$
 komega_bicg_init (N_H, N_L, N_z, x, z, itermax, threshold) start Allocate $v_3, v_5, \{\pi_k\}, \{\tau_k^{\mathrm{old}}\}, \{\mathbf{p}_k\}$ Copy $\{z_k\}$ If itermax $\neq 0$, allocate arrays to store α, β , and:math:/bf r /^/rm L / at each iteration. $v_4 = v_2^*$ (an arbitrary vector), $v_3 = v_5 = 0$, $\mathbf{p}_k = \mathbf{x}_k = \mathbf{0}(k = 1 \cdots N_z), \ \pi_k = \pi_k^{\mathrm{old}} = 1(k = 1 \cdots N_z)$ $\rho = \infty, \ \alpha = 1, z_{\mathrm{seed}} = 0$ ($v_2 \equiv r, v_3 \equiv r^{\mathrm{old}}, v_4 \equiv \tilde{r}, v_5 \equiv \tilde{r}^{\mathrm{old}}$.) komega_bicg_init finish do iteration
$$\mathbf{r}^L = \hat{P}^\dagger v_2$$

$$v_{12} = \hat{H}v_2, v_{14} = \hat{H}v_4 \text{ [Or } (v_{12}, v_{14}) = \hat{H}(v_2, v_4) \text{]}$$
 komega_bicg_update ($v_1^2, v_2^2, v_1^2, v_1^2, v_1^2, v_2^2, v_1^2, v_2^2, v_1^2, v_2^2, v_1^2, v_2^2, v_1^2, v_2^2, v_1^2, v_1^2, v_2^2, v_1^2, v_1^$

o Seed switch

Search k which gives the smallest
$$|\pi_k|$$
. $\to z_{\rm seed}$, $\pi_{\rm seed}$, $\pi_{\rm seed}^{\rm old}$

$$oldsymbol{v}_2 = oldsymbol{v}_2/\pi_{
m seed}, oldsymbol{v}_3 = oldsymbol{v}_3/\pi_{
m seed}^{
m old}, oldsymbol{v}_4 = oldsymbol{v}_4/\pi_{
m seed}^*, oldsymbol{v}_5 = oldsymbol{v}_5/\pi_{
m seed}^{
m old*}$$

$$\alpha = (\pi_{\text{seed}}^{\text{old}}/\pi_{\text{seed}})\alpha, \rho = \rho/(\pi_{\text{seed}}^{\text{old}}\pi_{\text{seed}}^{\text{old}})$$

$$\{\pi_k = \pi_k/\pi_{\text{seed}}, \ \pi_k^{\text{old}} = \pi_k^{\text{old}}/\pi_{\text{seed}}^{\text{old}}\}$$

komega_bicg_update finish

if(status(1) < 0 (This indicates $|v_2|$ < Threshold)) exit

end do iteration

komega_bicg_finalize start

Deallocate
$$v_4, v_5, \{\pi_k\}, \{\pi_k^{\text{old}}\}, \{\mathbf{p}_k\}$$

komega_bicg_finalize finish

3.2 The schematic workflow of shifted COCG library

Allocate
$$oldsymbol{v}_1, oldsymbol{v}_2, \{\mathbf{x}_k\}, \mathbf{r}^{\mathrm{L}} \ oldsymbol{v}_2 = oldsymbol{arphi}_j$$

Allocate
$$v_3$$
, $\{\pi_k\}$, $\{\pi_k^{\text{old}}\}$, $\{\mathbf{p}_k\}$

Copy
$$\{z_k\}$$

If itermax \neq 0, allocate arrays to store α , β , and \mathbf{r}^{L} .

$$v_3 = 0$$

$$\mathbf{p}_k = \mathbf{x}_k = \mathbf{0}(k = 1 \cdots N_z), \ \pi_k = \pi_k^{\text{old}} = 1(k = 1 \cdots N_z)$$

$$\rho=\infty,\ \alpha=1,\ \beta=0,\ z_{\rm seed}=0$$

(
$$\boldsymbol{v}_2 \equiv \boldsymbol{r}, \boldsymbol{v}_3 \equiv \boldsymbol{r}^{\mathrm{old}}$$
.)

komega_cocg_init finish

do iteration

$$\mathbf{r}^{\mathrm{L}} = \hat{P}^{\dagger} \mathbf{v}_{2}$$

$$\mathbf{v}_1 = \hat{H}\mathbf{v}_2$$

 $komega_cocg_update(v_1, v_2, x, r_small, status)$ start

o Seed equationw

$$\rho^{\text{old}} = \rho, \ \rho = \boldsymbol{v}_2 \cdot \boldsymbol{v}_2$$

$$\beta = \rho/\rho^{\rm old}$$

$$\boldsymbol{v}_1 = z_{\mathrm{seed}} \boldsymbol{v}_2 - \boldsymbol{v}_1$$

$$\alpha^{\text{old}} = \alpha, \ \alpha = \frac{\rho}{\mathbf{v}_2 \cdot \mathbf{v}_1 - \beta \rho / \alpha}$$

Shifted equations

do
$$k = 1 \cdots N_z$$

$$\begin{split} \pi_k^{\mathrm{new}} &= [1 + \alpha(z_k - z_{\mathrm{seed}})] \pi_k - \frac{\alpha\beta}{\alpha^{\mathrm{old}}} (\pi_k^{\mathrm{old}} - \pi_k) \\ \mathbf{p}_k &= \frac{1}{\pi_k} \mathbf{r}^{\mathrm{L}} + \frac{\pi_k^{\mathrm{old}} \pi_k^{\mathrm{old}}}{\pi_k \pi_k} \beta \mathbf{p}_k \\ \mathbf{x}_k &= \mathbf{x}_k + \frac{\pi_k}{\pi_k^{\mathrm{new}}} \alpha \mathbf{p}_k \\ \pi_k^{\mathrm{old}} &= \pi_k, \ \pi_k = \pi_k^{\mathrm{new}} \\ \text{end do } k \\ v_1 &= \left(1 + \frac{\alpha\beta}{\alpha^{\mathrm{old}}}\right) v_2 - \alpha v_1 - \frac{\alpha\beta}{\alpha^{\mathrm{old}}} v_3 \\ v_3 &= v_2, v_2 = v_1 \\ \circ \mathrm{Seed} \ \mathrm{switch} \\ \mathrm{Search} \ k \ \mathrm{which} \ \mathrm{gives} \ \mathrm{the} \ \mathrm{smallest} \ |p_i_k| \ . \to z_{\mathrm{seed}}, \ \pi_{\mathrm{seed}}, \ \pi_{\mathrm{seed}} \\ \alpha &= (\pi_{\mathrm{seed}}^{\mathrm{old}} / \pi_{\mathrm{seed}}) \alpha, \ \rho = \rho / (\pi_{\mathrm{seed}}^{\mathrm{old}} \pi_{\mathrm{seed}}^{\mathrm{old}}) \\ \{\pi_k &= \pi_k / \pi_{\mathrm{seed}}, \ \pi_k^{\mathrm{old}} = \pi_k^{\mathrm{old}} / \pi_{\mathrm{seed}}^{\mathrm{old}} \} \\ \mathrm{komega_cocg_update} \ \mathrm{finish} \\ \mathrm{if}(\mathrm{status}(1) < 0 \ (\mathrm{This} \ \mathrm{indicates} \ |v_2| < \mathrm{Threshold.})) \ \mathrm{exit} \end{split}$$

end do iteration

komega_cocg_finalize start

Deallocate v_3 , $\{\pi_k\}$, $\{\pi_k^{\mathrm{old}}\}$, $\{\mathbf{p}_k\}$

komega_cocg_finalize finish

3.3 The schematic workflow of shifted CG library

The workflow is the same as that of the shifted COCG library.

Install

4.1 Overall procedure

First, please type

```
$ ./configure --prefix=install_dir
```

Then, this script checks the compiler and the libraries required for the installation, and creates Makefiles. install_dir indicates the full path of the directory where the library is installed (you should replace it according to your case). If none is specified, /use/local/ is chosen for storing libraries by make install (Therefore, if one is not the admin, install_dir must be specified to the different directory). configure has many options, and they are used according to the environment etc. For more details, please see *Options for configure*.

After configure finishes successfully and Makefiles are generated, please type

```
$ make
```

to build libraries. Then please type

```
$ make install
```

to store libraries and the sample program to install_dir/lib and install_dir/bin, respectively. Although one can use libraries and the sample program without make install, they are a little different to the installed one.

Add the $K\omega$ library directory (install_dir/lib) to the search path of the dynamically linked program (environment variable LD_LIBRARY_PATH).

```
$ export LD_LIBRARY_PATH=${LD_LIBRARY_PATH}:install_dir/lib
```

4.2 Options for configure

configure has many options and environment variables. They can be specified at once. E.g.

```
$ ./configure --prefix=/home/komega/ --with-mpi=yes FC=mpif90
```

All options and variables have default values. We show a part of them as follows:

```
---prefix

Default: ---prefix=/usr/local/. Specify the directory where the library etc. are installed.

--with-mpi
```

Default: --with-mpi=no (without MPI). Whether use MPI (--with-mpi=yes), or not.

--with-openmp

--enable-shared

Default: --enable-shared. Whether generate shared library.

--enable-static

Default: --enable-static. Whether generate static library.

--disable-zdot

Default: --enable-zdot. When ZDOTC and ZDOTU in BLAS do not work correctly (e.g. standard BLAS in MacOSX), please use this option to be disable these functions.

--enable-threadsafe

Default: --disable-threadsafe. If you want to call $K\omega$ routine in the parallel region (i.e. plan to solve different equations among threads), please use this option (**Experimental**).

FC

Default: The fortran compiler chosen automatically from those in the system. When <code>--with-mpi</code> is specified, the corresponding MPI compiler (such as <code>mpif90</code>) is searched. If FC printed the end of the standard-output of <code>configure</code> is not what you want, please set it manually as <code>./configure</code> <code>FC=qfortran</code>.

--help

Display all options including above, and stop without configuration.

Usage

The calculation is done to utilize functions by the following procedures.

- Initialization (* *init*)
- Update results iteratively (*_update)
- (Optional) Take the information for the restart (*_getcoef, *_getvec)
- Finalization (*_finalize)

The restart calculation can be done by the following procedures.

- Initialization with the information of the previous calculation (*_restart)
- Update results iteratively (*_update)
- (Optional) Take the information for the further restart (*_getcoef, *_getvec)
- Finalization (* *finalize*)

Warning: Since $K\omega$ is **not** thread safe, these routine must be called from the outside of the OpenMP-parallel region. If you want to call $K\omega$ routine in the parallel region (i.e. plan to solve different equations among threads), please use --enable-threadsafe option of configure (**Experimental**).

For FORTRAN, the modules can be called by

```
USE komega_cg_r ! Conjugate-gradient method for real vectors
USE komega_cg_c ! Conjugate-gradient method for complex vectors
USE komega_cocg ! Conjugate-orthogonal conjugate-gradient mehod
USE komega_bicg ! Biconjugate-gradient method
```

When we call $K\omega$ from C/C++ codes, we should include the header file as

```
#include komega.h
```

Scalar arguments should be passed as pointers. For MPI/Hybrid parallelized routine, the above line becomes Also, the communicator argument for the routine should be transformed from the C/C++'s one to the fortran's one as follows.

```
comm_f = MPI_Comm_c2f(comm_c);
```

5.1 Details of each routines

5.1.1 * init

Set and initialize internal variables in libraries. These routines should be called first before solving the shifted equation.

Syntax

Fortran

```
CALL komega_cg_r_init(ndim, nl, nz, x, z, itermax, threshold, comm)

CALL komega_cg_c_init(ndim, nl, nz, x, z, itermax, threshold, comm)

CALL komega_cocg_init(ndim, nl, nz, x, z, itermax, threshold, comm)

CALL komega_bicg_init(ndim, nl, nz, x, z, itermax, threshold, comm)

C/C++

komega_cg_r_init(&ndim, &nl, &nz, x, z, &itermax, &threshold, &comm);
komega_cg_c_init(&ndim, &nl, &nz, x, z, &itermax, &threshold, &comm);
komega_cocg_init(&ndim, &nl, &nz, x, z, &itermax, &threshold, &comm);
komega_bicg_init(&ndim, &nl, &nz, x, z, &itermax, &threshold, &comm);
```

Parameters

```
INTEGER, INTENT(IN) :: ndim
```

The dimension of solution vectors for the linearized equation. ndim for the dimension of variables in other routine is equal to this.

```
INTEGER, INTENT(IN) :: nl
```

The dimension of projected solution vectors. nl for the dimension of variables in other routine is equal to this.

```
INTEGER, INTENT(IN) :: nz
```

The number of shifted points. nz for the dimension of variables in other routine is equal to this

```
REAL(8),INTENT(OUT) :: x(nl*nz) ! (for "CG_R_init", "CG_C_init")
COMPLEX(8),INTENT(OUT) :: x(nl*nz) ! (for other cases)
```

The solution vector. In this procedure, 0 vector is returned.

```
REAL(8),INTENT(IN) :: z(nz) ! (for "CG_R_init", "CG_C_init")
COMPLEX(8),INTENT(IN) :: z(nz) ! (for other cases)
```

Shifted points.

```
INTEGER, INTENT(IN) :: itermax
```

The maximum iteration number for allocating arrays for the restart calculation. When itermax=0, these arrays are not allocated, and the restart calculation described later becomes unavailable.

```
REAL(8), INTENT(IN) :: threshold
```

The threshold value for the convergence determination. When the 2-norm of the residual vector for the seed equation becomes smaller than this value, the calculation is finished.

```
INTEGER, INTENT(IN), OPTIONAL :: comm
```

Optional argument. Communicators for MPI such as MPI_COMM_WORLD. Only for MPI / Hybrid parallelization. For C compiler, just pass NULL to omit this argment.

5.1.2 * restart

For the restart calculation, these routines are used instead of *_init. Set and initialize internal variables in libraries. These routines should be called first before solving the shifted equation.

Syntax

```
Fortran
```

```
CALL komega_cg_r_restart(ndim, nl, nz, x, z, itermax, threshold, status, &
                  iter_old, v2, v12, alpha_save, beta_save, z_seed, r_l_save, comm)
CALL komega_cg_c_restart(ndim, nl, nz, x, z, itermax, threshold, status, &
                  iter_old, v2, v12, alpha_save, beta_save, z_seed, r_l_save, comm)
CALL komega_cocg_restart(ndim, nl, nz, x, z, itermax, threshold, status, &
                  iter_old, v2, v12, alpha_save, beta_save, z_seed, r_l_save, comm)
CALL komega_bicg_restart(ndim, nl, nz, x, z, itermax, threshold, status, &
                 iter_old, v2, v12, v4, v14, alpha_save, beta_save, &
                  z_seed, r_l_save, comm)
δ
C/C++
komega_cg_r_restart(&ndim, &nl, &nz, x, z, &itermax, &threshold, status, &
                  &iter_old, v2, v12, alpha_save, beta_save, &z_seed, r_l_save, &comm);
komega_cg_c_restart(&ndim, &nl, &nz, x, z, &itermax, &threshold, status, &
                  &iter_old, v2, v12, alpha_save, beta_save, &z_seed, r_l_save, &comm);
komega_cocg_restart(&ndim, &nl, &nz, x, z, &itermax, &threshold, status, &
                 &iter_old, v2, v12, alpha_save, beta_save, &z_seed, r_l_save, &comm);
komega_bicg_restart(&ndim, &nl, &nz, x, z, &itermax, &threshold, status, &
                  &iter_old, v2, v12, v4, v14, alpha_save, beta_save, &
                  &z_seed, r_l_save, &comm);
```

Parameters

```
INTEGER, INTENT(IN) :: ndim
INTEGER, INTENT(IN) :: nl
INTEGER, INTENT(IN) :: nz
REAL(8), INTENT(OUT) :: x(nl*nz)
REAL(8), INTENT(IN) :: z(nz) ! (for "CG_R_restart", "CG_C_restart")
COMPLEX(8), INTENT(IN) :: z(nz) ! (Other)
INTEGER, INTENT(IN) :: itermax
REAL(8), INTENT(IN) :: threshold
INTEGER, INTENT(IN), OPTIONAL :: comm
```

The definition is same as *_init. See the parameters in *_init.

```
INTEGER, INTENT(OUT) :: status(3)
```

The error code is returned.

```
First component(status (1))
```

If the solution is converged or a breakdown occurs, the current total number of iteration with the minus sign is returned. In other cases, this routine returns the current total number of iteration. The calculation is continuable only when status (1)

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is the positive value; otherwise the result is meaningless even if the calculation is continued.

Second component(status(2))

1 is returned if itermax is set as a finite value and the convergence condition is not satisfied at the itermax-th iteration. 2 is returned if α diverges. 3 is returned if $\pi_{\rm seed}$ becomes 0. In the case of COCG_restart or BiCG_restart, 4 is returned if the residual vector and the shadow residual vector are orthogonal. In other cases, 0 is returned.

Third component(status (3))

The index of the seed point is returned.

```
INTEGER, INTENT(IN) :: iter_old
```

The number of iteration for the previous calculation.

```
REAL(8), INTENT(IN) :: v2(ndim) ! (for "CG_R_restart")
COMPLEX(8), INTENT(IN) :: v2(ndim) ! (Other)
```

The residual vector at the last step for the previous calculation.

```
REAL(8),INTENT(IN) :: v12(ndim) ! (for "CG_R_restart")
COMPLEX(8),INTENT(IN) :: v12(ndim) ! (Other)
```

The residual vector at the second from the last step for the previous calculation.

```
REAL(8),INTENT(IN) :: alpha_save(iter_old) ! (for "CG_R_restart", "CG_C_restart")
COMPLEX(8),INTENT(IN) :: alpha_save(iter_old) ! (Other)
```

The parameters α obtained by the previous calculation at each steps by (Bi)CG methods.

```
REAL(8), INTENT(IN) :: beta_save(iter_old) ! (for "CG_R_restart", "CG_C_restart")
COMPLEX(8), INTENT(IN) :: beta_save(iter_old) ! (Other)
```

The parameters β obtained by the previous calculation at each steps by (Bi)CG methods.

```
REAL(8),INTENT(IN) :: z_seed ! (for "CG_R_restart", "CG_C_restart")
COMPLEX(8),INTENT(IN) :: z_seed ! (Other)
```

The value of the seed shift for the previous calculation.

```
REAL(8),INTENT(IN) :: r_l_save(nl,iter_old) ! (for "CG_R_restart")
COMPLEX(8),INTENT(IN) :: r_l_save(nl,iter_old) ! (Other)
```

The projected residual vector at each iteration for the previous calculation.

```
REAL(8), INTENT(IN) :: v4(ndim) ! (for "CG_R_restart")
COMPLEX(8), INTENT(IN) :: v4(ndim) ! (Other)
```

The shadow residual vector at the last step for the previous calculation.

```
REAL(8),INTENT(IN) :: v14(ndim) ! (for "CG_R_restart")
COMPLEX(8),INTENT(IN) :: v14(ndim) ! (Other)
```

The shadow residual vector at the second last step for the previous calculation.

5.1.3 *_update

It is called alternately with the matrix-vector product in the loop and updates the solution.

Syntax

Fortran

```
CALL komega_cg_r_update(v12, v2, x, r_l, status)

CALL komega_cg_c_update(v12, v2, x, r_l, status)

CALL komega_cocg_update(v12, v2, x, r_l, status)

CALL komega_bicg_update(v12, v2, v14, v4, x, r_l, status)

C/C++

komega_cg_r_update(v12, v2, x, r_l, status);

komega_cg_c_update(v12, v2, x, r_l, status);

komega_ccg_update(v12, v2, x, r_l, status);

komega_bicg_update(v12, v2, v14, v4, x, r_l, status);
```

Parameters

```
REAL(8),INTENT(INOUT) :: v12(ndim) ! (for "CG_R_update")
COMPLEX(8),INTENT(INOUT) :: v12(ndim) ! (Other)
```

The product of the residual vector (v2) and the matrix. This routine returns the 2-norm of the updated residual vector as a first element of this array. This returned value is used, for examples, for printing the convergence profile.

```
REAL(8),INTENT(INOUT) :: v2(ndim) ! (for "CG_R_update")
COMPLEX(8),INTENT(INOUT) :: v2(ndim) ! (Other)
```

The residual vector is input and the updated residual vector is output.

```
REAL(8), INTENT(IN) :: v14(ndim) ! (for "CG_R_update")
COMPLEX(8), INTENT(IN) :: v14(ndim) ! (Other)
```

The product of the shadow residual vector (v4) and the matrix is input.

```
REAL(8), INTENT(INOUT) :: v4(ndim) ! (for "CG_R_update")
COMPLEX(8), INTENT(INOUT) :: v4(ndim) ! (Other)
```

The shadow residual vector is input and the updated vector is output.

```
INTEGER, INTENT(OUT) :: status(3)
```

The error code is returned.

```
First component (status (1))
```

If the solution is converged or a breakdown occurs, the current total number of iteration with the minus sign is returned. In other cases, this routine returns the current total number of iteration. The calculation is continuable only when status(1) is the positive value; otherwise the result is meaningless even if the calculation is continued.

Second component (status (2))

1 is returned if itermax is set as a finite value in the *_init routine and the convergence condition is not satisfied at the itermax-th iteration. 2 is returned if α diverges. 3 is returned if $\pi_{\rm seed}$ becomes 0. In the case of COCG_update or BiCG_update, 4 is returned if the residual vector and the shadow residual vector are orthogonal. In other cases, 0 is returned.

Third component (status (3))

The index of the seed point is returned.

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5.1.4 *_getcoef

Get the coefficients used in the restart calculation. To call these routines, itermax in * init routine must not be 0.

The total number of iteration (iter_old) used in this routine is computed by using status which is an output of *_update as follows:

```
iter_old = ABS(status(1))
Syntax
    Fortran
    CALL komega_cg_r_getcoef (alpha_save, beta_save, z_seed, r_l_save)
    CALL komega_cq_c_getcoef (alpha_save, beta_save, z_seed, r_l_save)
    CALL komega_cocg_getcoef (alpha_save, beta_save, z_seed, r_l_save)
    CALL komega_bicg_getcoef(alpha_save, beta_save, z_seed, r_l_save)
    C/C++
    komega_cg_r_getcoef(alpha_save, beta_save, &z_seed, r_l_save);
    komega_cg_c_getcoef(alpha_save, beta_save, &z_seed, r_l_save);
    komega_cocg_getcoef(alpha_save, beta_save, &z_seed, r_l_save);
    komega_bicg_getcoef(alpha_save, beta_save, &z_seed, r_l_save);
Parameters
    REAL(8), INTENT(OUT) :: alpha_save(iter_old) ! (for "CG_R_restart", "CG_C_restart")
    COMPLEX(8), INTENT(OUT) :: alpha_save(iter_old) ! (Other)
         The parameters \alpha of the (Bi)CG method at each iteration.
    REAL(8), INTENT(OUT) :: beta_save(iter_old) ! (for "CG_R_restart", "CG_C_restart")
    COMPLEX(8), INTENT(OUT) :: beta_save(iter_old) ! (Other)
         The parameters \beta of the (Bi)CG method at each iteration.
    REAL(8), INTENT(OUT) :: z_seed ! (for "CG_R_restart", "CG_C_restart")
    COMPLEX(8), INTENT(OUT) :: z_seed ! (Other)
         Seed shift.
```

The projected residual vectors at each iteration.

REAL(8),INTENT(IN) :: r_l_save(nl,iter_old) ! ("CG_R_restart")
COMPLEX(8),INTENT(IN) :: r_l_save(nl,iter_old) ! (Other)

5.1.5 * getvec

Get the residual vectors to use the restart calculation. To call these routines, itermax in the *_init routine must not be 0.

Syntax

```
Fortran
```

```
CALL komega_cg_r_getvec(r_old)
CALL komega_cg_c_getvec(r_old)
CALL komega_cocg_getvec(r_old)
CALL komega_bicg_getvec(r_old, r_tilde_old)
```

```
C/C++

komega_cg_r_getvec(r_old);
komega_cg_c_getvec(r_old);
komega_cocg_getvec(r_old);
komega_bicg_getvec(r_old, r_tilde_old);

Parameters

REAL(8), INTENT(OUT) :: r_old(ndim) ! (for "CG_R_getvec")
COMPLEX(8), INTENT(OUT) :: r_old(ndim) ! (Other)

The residual vector at the second last step in the previous calculation.

COMPLEX(8), INTENT(OUT) :: r_tilde_old(ndim)
```

The shadow residual vector at the second last step in the previous calculation.

5.1.6 *_getresidual

Get the values of 2-norm of the residual vector at each shift points. These routines can be called from anywhere between *_init and *_finalize . These routines do not affect the calculation results.

Syntax

```
Fortran
```

```
CALL komega_cg_r_getresidual(res)
CALL komega_cg_c_getresidual(res)
CALL komega_cocg_getresidual(res)
CALL komega_bicg_getresidual(res)
C/C++
komega_cg_r_getresidual(res);
komega_cg_c_getresidual(res);
komega_cocg_getresidual(res);
komega_cocg_getresidual(res);
```

Parameters

```
COMPLEX(8), INTENT(OUT) :: res(nz)
```

The values of 2-norm of the residual vector at each shift points are returned.

5.1.7 *_finalize

Release memories of the arrays stored in the library.

Syntax

```
Fortran
```

```
CALL komega_cg_r_finalize()
CALL komega_cg_c_finalize()
CALL komega_cocg_finalize()
CALL komega_bicg_finalize()
C/C++
```

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```
komega_cg_r_finalize();
komega_cg_c_finalize();
komega_cocg_finalize();
komega_bicg_finalize();
```

5.2 Sample codes for using shifted BiCG library

As a typical example, the usage of shifted BiCG library is shown below.

```
PROGRAM my_proq
  USE komega_bicg, ONLY : komega_bicg_init, komega_bicg_restart, &
                           komega_bicg_update, komega_bicg_getcoef, &
                           komega_bicg_getvec, komega_bicg_finalize
  USE solve_cc_routines, ONLY : input_size, input_restart, &
                                 projection, &
                                 hamiltonian_prod, generate_system, &
                                 output_restart, output_result
  IMPLICIT NONE
  INTEGER, SAVE :: &
  & ndim, & ! Size of Hilvert space
 & nz, & ! Number of frequencies & nl, & ! Number of Left vector
  & itermax, & ! Max. number of iteraction
  & iter_old ! Number of iteraction of previous run
  REAL(8), SAVE :: &
  & threshold ! Convergence Threshold
  COMPLEX(8), SAVE :: &
  & z_seed ! Seed frequency
  COMPLEX(8), ALLOCATABLE, SAVE :: &
             ! (nz): Frequency
  COMPLEX(8), ALLOCATABLE, SAVE :: &
  & ham(:,:), &
  & rhs(:), &
  & v12(:), v2(:), & ! (ndim): Working vector
  & v14(:), v4(:), & ! (ndim): Working vector
  & r_l(:), & ! (nl) : Projected residual vector
  & x(:,:) ! (nl,nz) : Projected result
  ! Variables for Restart
  COMPLEX(8), ALLOCATABLE, SAVE :: &
  & alpha(:), beta(:) ! (iter_old)
  COMPLEX(8), ALLOCATABLE, SAVE :: &
  & r_l_save(:,:) ! (nl,iter_old) Projected residual vectors
  ! Variables for Restart
  INTEGER :: &
```

```
& iter, & ! Counter for Iteration
& status(3)
LOGICAL :: &
& restart_in, & ! If .TRUE., sestart from the previous result
& restart_out ! If .TRUE., save datas for the next run
! Input Size of vectors, numerical conditions
CALL input_size(ndim, nl, nz)
CALL input_condition(itermax, threshold, restart_in, restart_out)
ALLOCATE (v12 (ndim), v2 (ndim), v14 (ndim), v4 (ndim), r_1 (nl), &
         x(nl,nz), z(nz), ham(ndim,ndim), rhs(ndim))
CALL generate_system(ndim, ham, rhs, z)
WRITE ( * , * )
WRITE (*,*) "##### CG Initialization #####"
WRITE ( * , * )
{\tt IF} \, ({\tt restart\_in}) \,\,\, {\tt THEN}
 1
  CALL input_restart(iter_old, zseed, alpha, beta, r_l_save)
  IF (restart_out) THEN
     CALL komega_bicg_restart( &
         ndim, nl, nz, x, z, itermax, threshold, &
     &
          status, iter_old, v2, v12, v4, v14, alpha, &
     &
     &
         beta, z_seed, r_l_save)
  ELSE
     CALL komega_bicg_restart ( &
     &
         ndim, nl, nz, x, z, 0, threshold, &
     &
          status, iter_old, v2, v12, v4, v14, alpha, &
     &
          beta, z_seed, r_l_save)
  END IF
  ! These vectors were saved in BiCG routine
  DEALLOCATE (alpha, beta, r_l_save)
  IF (status (1) /= 0) GOTO 10
ELSE
   !
   ! Generate Right Hand Side Vector
   v2(1:ndim) = rhs(1:ndim)
   v4(1:ndim) = CONJG(v2(1:ndim))
   !v4(1:ndim) = v2(1:ndim)
   IF (restart_out) THEN
      CALL komega_bicg_init(ndim, nl, nz, x, z, termax, threshold)
   ELSE
      CALL komega_bicg_init(ndim, nl, nz, x, z, 0, threshold)
   END IF
END IF
```

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```
! BiCG Loop
WRITE ( * , * )
WRITE(*,*) "##### CG Iteration #####"
WRITE (*, *)
DO iter = 1, itermax
   ! Projection of Residual vector into the space
   ! spaned by left vectors
   r_1(1:nl) = projection(v2(1:nl))
   ! Matrix-vector product
   CALL hamiltonian_prod(Ham, v2, v12)
   CALL hamiltonian_prod(Ham, v4, v14)
   ! Update result x with BiCG
   CALL komega_bicg_update(v12, v2, v14, v4, x, r_l, status)
   WRITE(*,'(a,i,a,3i,a,e15.5)') "lopp : ", iter, &
                                  ", status : ", status(1:3), &
                                  ", Res. : ", DBLE(v12(1))
   IF (status(1) < 0) EXIT</pre>
END DO
IF (status(2) == 0) THEN
  WRITE(*,*) " Converged in iteration ", ABS(status(1))
ELSE IF(status(2) == 1) THEN
  WRITE(*,*) " Not Converged in iteration ", ABS(status(1))
ELSE IF(status(2) == 2) THEN
  WRITE (*,*) " Alpha becomes infinity", ABS (status (1))
ELSE IF(status(2) == 3) THEN
  WRITE(*,*) " Pi_seed becomes zero", ABS(status(1))
ELSE IF(status(2) == 4) THEN
WRITE (*, *) " Residual & Shadow residual are orthogonal", &
          ABS (status (1))
END IF
! Total number of iteration
iter_old = ABS(status(1))
! Get these vectors for restart in the Next run
IF (restart_out) THEN
  1
   ALLOCATE (alpha (iter_old), beta (iter_old), r_l_save (nl, iter_old))
   CALL komeqa_bicq_getcoef(alpha, beta, z_seed, r_l_save)
   CALL komega_bicg_getvec(v12, v14)
   CALL output_restart(iter_old, z_seed, alpha, beta, &
                       r_l_save, v12, v14)
```

```
!
DEALLOCATE (alpha, beta, r_l_save)
!
END IF
!
10 CONTINUE
!
! Deallocate all intrinsic vectors
!
CALL komega_bicg_finalize()
!
! Output to a file
!
CALL output_result(nl, nz, z, x, r_l)
!
DEALLOCATE(v12, v2, v14, v4, r_l, x, z)
!
WRITE(*,*)
WRITE(*,*)
!
END PROGRAM my_prog
```

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Re-distribution of this library

6.1 Contain Komega in your program

 $K\omega$ library is distributed with the Lesser General Public License (LGPL). It is summarized as follows:

- $K\omega$ can be freely distributed, modified, copied and pasted, in a private program (in the research group, coworkers, etc.).
- For the released program (open-source, free, commercial software etc.):
 - When you contain the source-code of $K\omega$ (either as is and modified) in the distributed source code of your program, please distribute your program with LGPL/GPL.
 - If you do not include the source-code of $K\omega$ (just call it), you can freely distribute your program with any licenses.
 - If you distribute a binary file which is statically linked to $K\omega$ library, please use LGPL/GPL. However, if you distribute a binary file which is dynamically linked to $K\omega$ library (therefore $K\omega$ itself is not contained), you can freely distribute your binary file with any licenses.

6.2 Build Komega without Autoconf

In this package, $K\omega$ is built with Autotools (Autoconf, Automake, Libtool). If you do not want to use Autotools for your distributed program with $K\omega$ source, you can use the following simple Makefile (please care about TAB).

```
F90 = gfortran

FFLAGS = -fopenmp -g -O2 #-D__MPI -D__NO_ZDOT -D__KOMEGA_THREAD

.SUFFIXES:
.SUFFIXES: .o.F90

OBJS = \
komega_cg_c.o \
komega_cg_r.o \
komega_cocg.o \
komega_bicg.o \
komega_bicg.o \
komega_math.o \
komega_vals.o

all:libkomega.a:$(OBJS)
```

```
ar cr libkomega.a $(OBJS)

.F90.o:
    $(F90) -c $< $(FFLAGS)

clean:
    rm -f *.o *.a *.mod

komega_cg_c.o:komega_math.o
komega_cg_r.o:komega_wals.o
komega_cg_r.o:komega_math.o
komega_cg_r.o:komega_wals.o
komega_cocg.o:komega_vals.o
komega_cocg.o:komega_wals.o
komega_cocg.o:komega_wals.o
komega_bicg.o:komega_wals.o
komega_bicg.o:komega_wals.o
komega_bicg.o:komega_wals.o
komega_math.o:komega_vals.o
komega_math.o:komega_vals.o
```

6.3 Lesser General Public License

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--disable-zdot, and --enable-thread of the options of configure, respectively.

You should have received a copy of the GNU Lesser General Public License along with this library; if not, write to the Free Software Foundation, Inc., 59 Temple Place, Suite 330, Boston, MA 02111-1307 USA

For more details, See 'COPYING.LESSER' in the root directory of this library.

Contact

If you have any comments, questions, bug reports etc. about this library, please contact to the main developer (Mitsuaki Kawamura) by sending the e-mail (the address is shown below).

```
mkawamura_at_issp.u-tokyo.ac.jp
```

Please change _at_ into @, when you will send the e-mail.

Reference

- [1] A. Frommer, Computing **70**, 87 (2003).
- [2] S. Yamamoto, T. Sogabe, T. Hoshi, S.-L. Zhang, and T. Fujiwara, J. Phys. Soc. Jpn. 77, 114713 (2008).