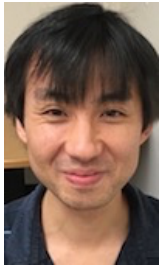


# 強磁性物質データベースの構築



物性研 福島グループ

櫻井誠大 (Masahiro Sakurai) sakurai@issp.u-tokyo.ac.jp

2015年4月–2020年3月 米国 テキサス大 ポスドク\*



- 第一原理計算
  - 磁性クラスター(実空間 DFT)
  - 結晶磁気異方性(平面波 DFT)
  - バンドギャップ(GW法)、光吸収スペクトル(GW+BSE法)
- 強磁性体データベース
  - 機械学習向け基礎データ



\* supported by the National Science Foundation (NSF)

# Contents

---

NSF–DMREF project

Three collaborative teams\* (theory & experiment)

Magnetic Materials Database

Data collection (known crystal structures)

Data generation (new structures & first-principles calculations)

Data organization (server applications, scripts, ...)

Unique features

Preliminary results

\*Most recent paper:

B. Bala., M. Sakurai, C.-Z. Wang, X. Xu, K.-M. Ho, J. R. Chelikowsky, and D. J. Sellmyer:  
“Synergistic Computational and Experimental Discovery of Novel Magnetic Materials”  
Molecular Systems Design & Engineering, 5, 1098-1117 (2020).  
<https://doi.org/10.1039/D0ME00050G>



# NSF-DMREF project (2014–2017–2020)

---

*“Collaborative Research  
for  
the Design and Synthesis of Novel Magnetic Materials”*

## The University of Texas at Austin [Theory]

James R. Chelikowsky



## RE-free magnetic materials

high magnetization ( $M_s$ )

high magnetic anisotropy ( $K$ )

high Curie temperature ( $T_c$ )

## Iowa State University (Ames Lab.) [Theory]

Kai-Ming Ho

Cai-Zhuang Wang



## Methods

DFT (PARSEC, QE, VASP)

Adaptive genetic algorithm

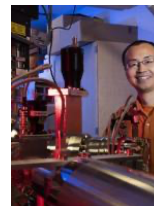
LMTO-ASA-GF

“Non-equilibrium” synthesis

## University of Nebraska–Lincoln [Experiment]

David J. Sellmyer

Xiaoshan Xu



## Joint work

joint papers

monthly Skype meeting

# Permanent magnet materials

## Permanent magnet

Key properties:

- (i) Saturation magnetization  $J_S$
- (ii) Coercivity  $H_c$  ( $\sim$  magnetic anisotropy  $K_1$ )
- (iii) Curie temperature  $T_C$

These rely strongly on rare-earth elements (Nd, Sm, Dy, ...)  $\leftarrow$  *potential supply risk!*

解説記事 「磁石の秘密」 赤井久純  
日本物理学会誌 71 (2016) 277-281.

母物質(固有特性)  
材料(界面、欠陥)  
磁石(焼結)

## Theoretical approach

*pseudopotential DFT plus machine-learning technique*



Basic inputs:

Composition:  $A_x B_y C_z$

Space group (symmetry)

Lattice parameters:  $\mathbf{a}, \mathbf{b}, \mathbf{c}$

Atomic positions:  $\{\mathbf{r}_i\}$

Site-specific quantities:

Magnetic moments:  $m_j$

Spin-orbit coupling:  $E_{\text{soc}}$

Exchange interaction:  $J_{ij}$

Key properties:

$J_S$

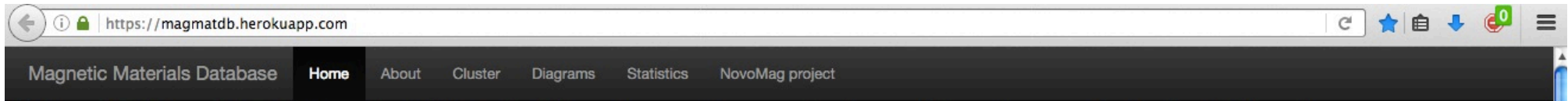
$K_1$

$T_C$



*New materials with desired properties*

# Magnetic Materials Database at <https://magmatdb.herokuapp.com>



**Database statistics:** a total of 3,826 entries, including 300+ Fe-based *rare-earth-free* magnets discovered through our [genetic algorithm](#) (GA) searches

**Phase diagrams** of binary phases: [Fe-N](#) (34 structures), [Fe-Si](#), [Fe-S](#), [Co-N](#) (183 structures), [Zr-Co](#) (42 structures)

**Phase diagrams** of ternary phases: [Fe-Co-N](#) (259 structures), [Fe-Co-S](#) (31 structures), [Zr-Co-X](#) (X=B,C,N; 176 structures),

Elements    
 random selection: [Co-N](#) (183 entries found)

Displaying 10 entries out of a total of 3,826 entries.

Materials ID	Crystal structure		Stability [Footnotes]					Magnetic properties [Footnotes, magnetic units]							References		
	Formula	Formula units per cell	Crystal system	Space group [Number]	Formation energy (eV/atom)	Energy relative to convex hull (eV/atom)	Synthesis	Averaged magnetic moment ( $\mu_B$ /atom)	Magnetic polarization, J (T)	Magnetic anisotropy constants $K^{a-c}$ , $K^{b-c}$ , $K^{b-a}$ , $K^{d-a}$				Magnetic easy axis	Curie temperature $T_C$ (K)	Methods	References
MMD-1	Fe	2	cubic	Im-3m [229]	0.000	0 (stable)	bcc Fe	2.23	2.18	0.00	0.00	0.00	0.01	a	953.2	DFT	mp-13
MMD-2	Co	2	hexagonal	P6_3/mmc [194]	0.000	0 (stable)	hcp Co	1.61	1.72	0.22	0.22	0.00	.	c	1474.2	DFT	mp-54
MMD-3	Ni	4	cubic	Fm-3m [225]	0.000	0 (stable)	fcc Ni	0.65	0.68	0.00	0.00	0.00	0.00	a	401.8	DFT	mp-23
MMD-4	FeCo <sub>5</sub> N <sub>2</sub>	2	monoclinic	C2 [5]	0.040	0.073	GA search	0.80	0.95	-0.29	-0.34	-0.05	.	b	.	DFT	DOI link

**ID**  
**Formula**

**Space group**

**Formation energy**

**Key magnetic properties:**  
 (1) magnetic moments  
 (2) magnetic anisotropy energy  
 (3) Curie temperature

**Methods**  
**References**

Search filters: elements, formula, space group, easy axis, ...

Available files: CIF, POSCAR, LAMMPS, JSON, YAML

<b>Open-access Materials Database</b>	<b>[1] Materials Project</b>	<b>[2] Open Quantum Materials Database</b>	<b>[3] Magnetic Materials Database</b>	<b>[4] Topological Material Database</b>
Team	UC Berkeley	Northwestern University	Texas, Iowa, Nebraska	Europe
Materials data				
# of entries	124,515	637,644	3,826	24,825
crystallography	✓	✓	✓	✓
phase stability	✓	✓	✓	—
Magnetism data				
magnetic moment	✓	—	✓	—
magnetic anisotropy	—	—	✓	—
Curie temperature	—	—	✓	—
Topological data				
Z indices, etc.	—	—	—	✓

[1] <https://materialsproject.org>

[2] <http://oqmd.org>

[3] <https://magmatdb.herokuapp.com>

[4] <https://www.topologicalquantumchemistry.org>



# Elements and Stats

Explore Materials [Advanced Search Syntax](#)

by Elements  search

<https://materialsproject.org/>

1	H																	2	He																								
3	Li	4	Be													5	B	6	C	7	N	8	O	9	F	10	Ne																
11	Na	12	Mg													13	Al	14	Si	15	P	16	S	17	Cl	18	Ar																
19	K	20	Ca	21	Sc	22	Ti	23	V	24	Cr	25	Mn	26	Fe	27	Co	28	Ni	29	Cu	30	Zn	31	Ga	32	Ge	33	As	34	Se	35	Br	36	Kr								
37	Rb	38	Sr	39	Y	40	Zr	41	Nb	42	Mo	43	Tc	44	Ru	45	Rh	46	Pd	47	Ag	48	Cd	49	In	50	Sn	51	Sb	52	Te	53	I	54	Xe								
55	Cs	56	Ba	57-71	La-Lu	72	Hf	73	Ta	74	W	75	Re	76	Os	77	Ir	78	Pt	79	Au	80	Hg	81	Tl	82	Pb	83	Bi	84	Po	85	At	86	Rn								
87	Fr	88	Ra	89-103	Ac-Lr	104	Rf	105	Db	106	Sg	107	Bh	108	Hs	109	Mt	110	Ds	111	Rg	112	Cn																				
		57	La	58	Ce	59	Pr	60	Nd	61	Pm	62	Sm	63	Eu	64	Gd	65	Tb	66	Dy	67	Ho	68	Er	69	Tm	70	Yb	71	Lu												
		89	Ac	90	Th	91	Pa	92	U	93	Np	94	Pu	95	Am	96	Cm	97	Bk	98	Cf	99	Es	100	Fm	101	Md	102	No	103	Lr												

**M** = Mn, Fe, Co, Ni

**X** = B, C, N, O;

Al, Si, P, S;

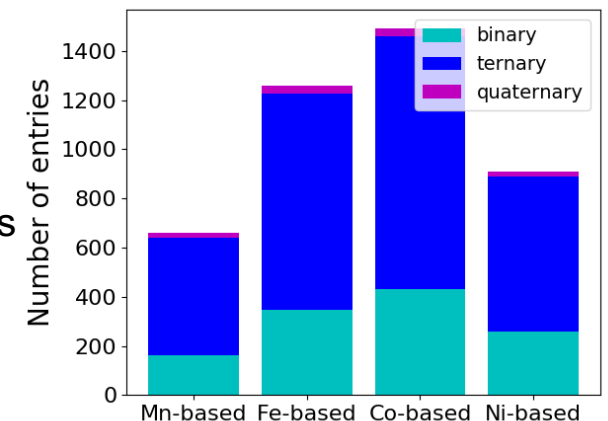
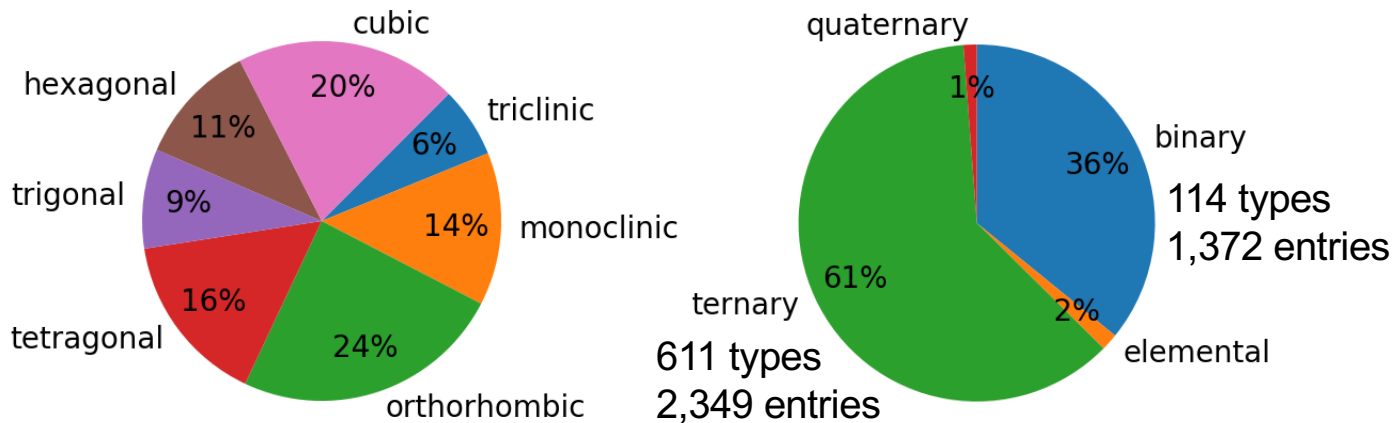
Ga, Ge, As, Se

**X** = Ti, V, Cr, Cu, Zn;

Y, Zr, Nb, Mo;

Pt

<https://magmatdb.herokuapp.com/stats>



# Adaptive Genetic Algorithm (AGA)

---

## How AGA works:

Step 1: initial seeds

8 slots in a pool



Step 2: relax with classical potentials  $\phi(r)$   
sort by energy (“rough guess”)

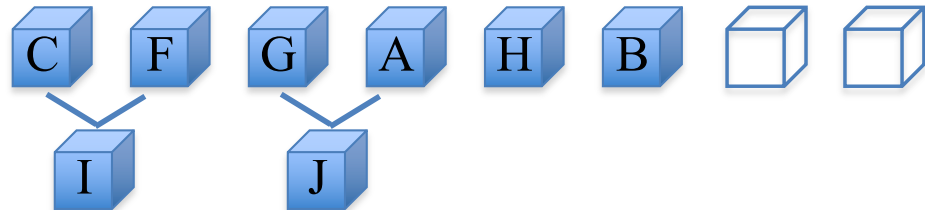


Step 3: refine with DFT (“adaptive”)  
update classical potentials

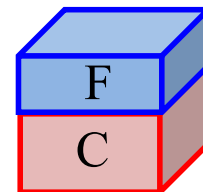
lowest 2 structures:

Energy  $E$ , Forces  $\{F_i\}$ , Stress  $\underline{S}$   $\rightarrow$   $\phi^{\text{new}}(r)$

Step 4: new generation



“cut-and-paste” mixing

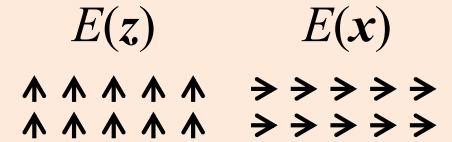




# Pseudopotential DFT

Magnetization & formation energy

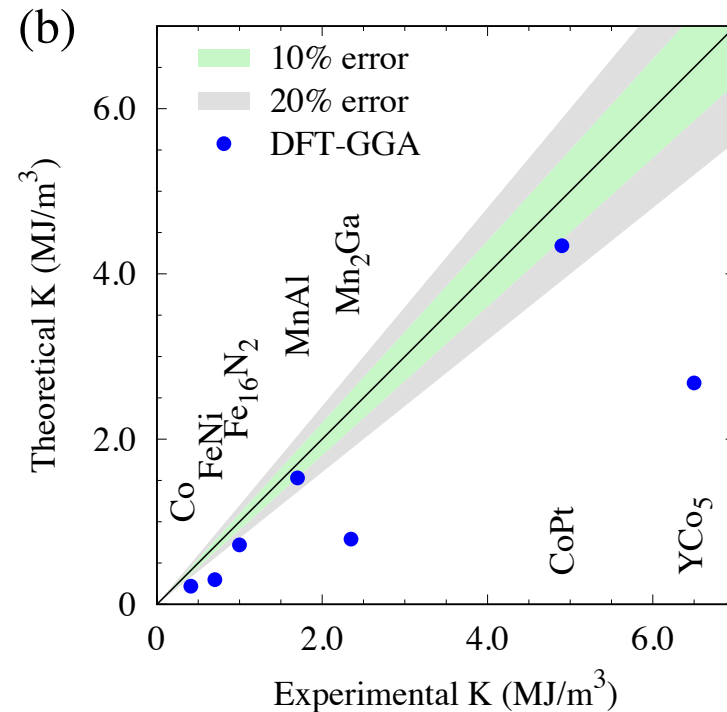
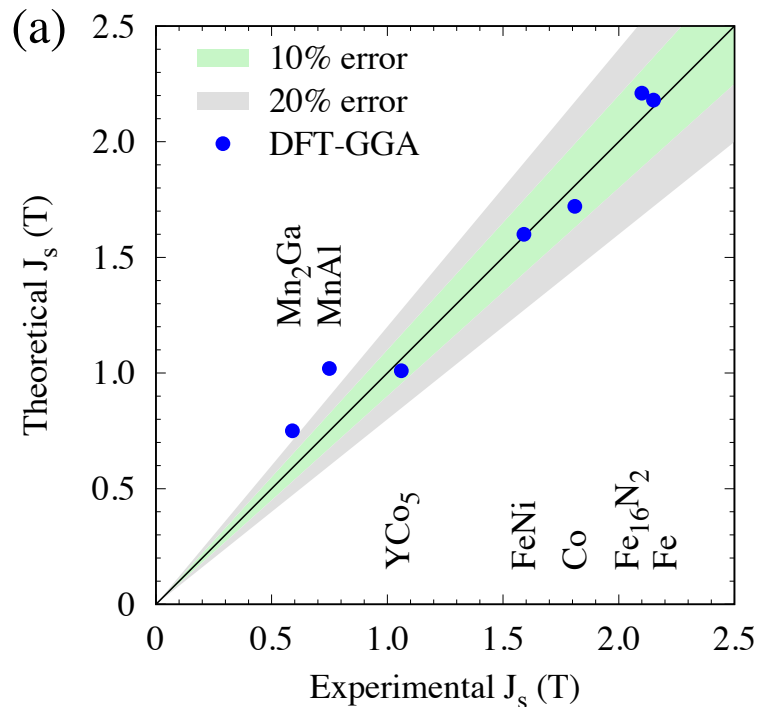
Spin-polarized calculations:  $\rho_{\text{up}} - \rho_{\text{dn}} \rightarrow$  moments, magnetization



Magnetic anisotropy energy (constant)

$$E_A = K_1 V \sin^2 \theta + K_2 V \sin^4 \theta + \dots = E_{\text{tot}}(\mathbf{x}) - E_{\text{tot}}(\mathbf{z}) \quad [\sim 1-10 \text{ meV per formula unit}]$$

$$K_1 = E_A / V \quad [\sim 1-10 \text{ MJ/m}^3]$$

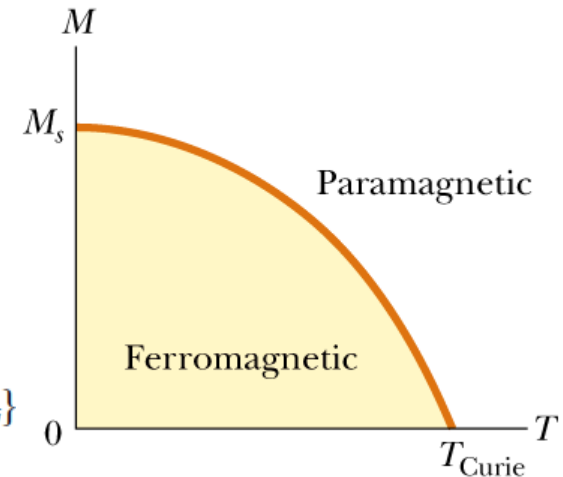


# Curie temperature $T_C$

Classical Heisenberg model  $H = -\sum_{ij} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$

Mean-field approximation  $T_C = 2/3 \sum_{ij} J_{ij}$

Exchange interactions  $J_{ij} = \frac{1}{2\pi} \int^{\epsilon_F} d\epsilon \times \text{Im Tr}_L \{ \delta P_i (T_{ij}^\dagger T_{ji}^\dagger + T_{ij}^\dagger T_{ji}^\dagger) \delta P_j \}$

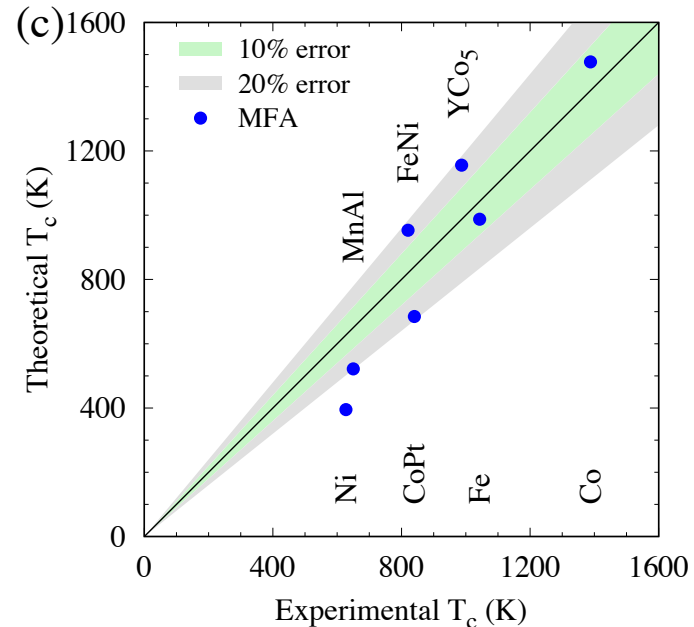


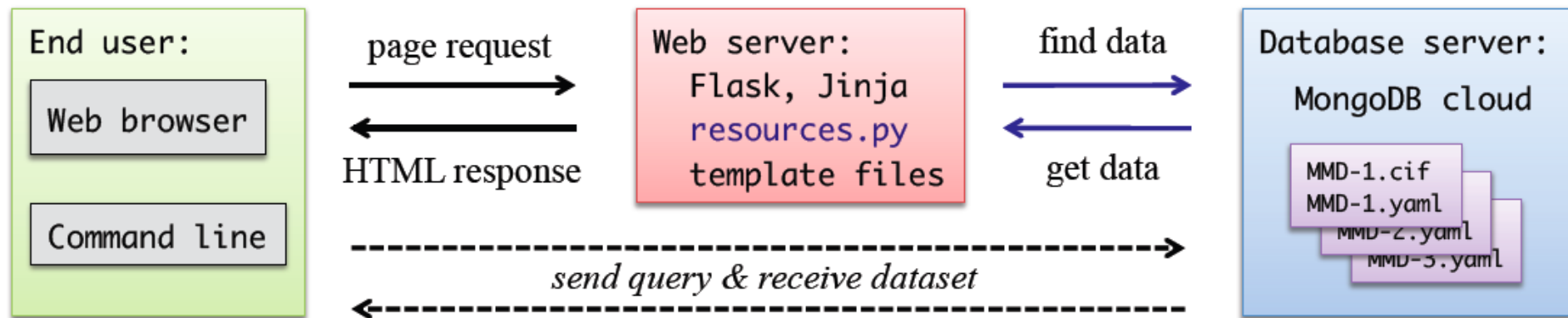
Linear muffin-tin method (LMTO)  
Green's function (GF) approach

J. Appl. Phys. 85, 4827 (1999)

QUESTALL (M. van Schilfgaarde)  
<https://www.questaal.org/>

*Works well to capture trends!*





Software	Role	URL
<b>Database</b>		
MongoDB	Database cloud	<a href="http://www.mongodb.com">www.mongodb.com</a>
Flask, Jinja	Web applications	<a href="http://palletsprojects.com/p/flask">palletsprojects.com/p/flask</a>
<b>Data entries</b>		
Pymatgen	Crystallographic data (CIF) Computed data (YAML)	<a href="http://pymatgen.org">pymatgen.org</a>
Adaptive GA	Crystal structure search	<a href="https://doi.org/10.1088/0953-8984/26/3/035402">doi.org/10.1088/0953-8984/26/3/035402</a>
Materials Project	Known structures	<a href="http://materialsproject.org">materialsproject.org</a>
<b>First-principles calculations</b>		
QE, VASP	DFT for $\Delta E_{\text{hull}}$ , $M_S$ , and $K_1$	<a href="http://quantum-espresso.org">quantum-espresso.org</a> + <a href="http://vasp.at">vasp</a>
PARSEC	DFT for clusters	<a href="http://real-space.org">real-space.org</a>
Qustaal	LMTO-GF for $T_C$ and $J_{ij}$	<a href="http://questaal.org">questaal.org</a>

# Data structure

```
- '@class': ComputedStructureEntry
  '@module': pymatgen.entries.computed_entries
  composition: !!python/object/apply:collections.defaultdict
    dictitems: {Fe: 2.0}
  data:
    critical_temperature:
      Curie_temperature: {unit: K, value: 953.2}
    formation_energy:
      above_hull: {unit: meV/atom, value: 0.0}
      decomposition: {unit: meV/atom, value: 0.0}
    magnetic_anisotropy:
      constant: {a-c: null, b-a: null, b-c: null, d-a: 0.009, unit: MJ/m^3}
      easy_axis: a
      energy: {a-c: null, b-a: null, b-c: null, d-a: 0.001, unit: meV/cell}
      parameters:
        kappa: 0.049
        kgrid: [22, 22, 22]
    magnetic_moment:
      magnetic_polarization: {unit: Tesla, value: 2.18}
      ordering: Ferromagnetic
      total_magnetic_moment: {unit: Bohr_magneton/atom, value: 2.21}
    :
    :
    :
```

← bcc\_Fe.yaml

# Data structure (continued)

structure:

'@class': Structure

'@module': pymatgen.core.structure

lattice:

a: 2.86944

← bcc\_Fe.cif

alpha: 90.0

b: 2.86944

beta: 90.0

c: 2.86944

gamma: 90.0

volume: 23.626067707920384

sites:

- abc: [0.0, 0.0, 0.0]

label: Fe

properties: {}

species:

- {element: Fe, occu: 1.0}

xyz: [0.0, 0.0, 0.0]

- abc: [0.5, 0.5, 0.5]

label: Fe

properties: {}

species:

- {element: Fe, occu: 1.0}

xyz: [1.43472, 1.43472, 1.43472]

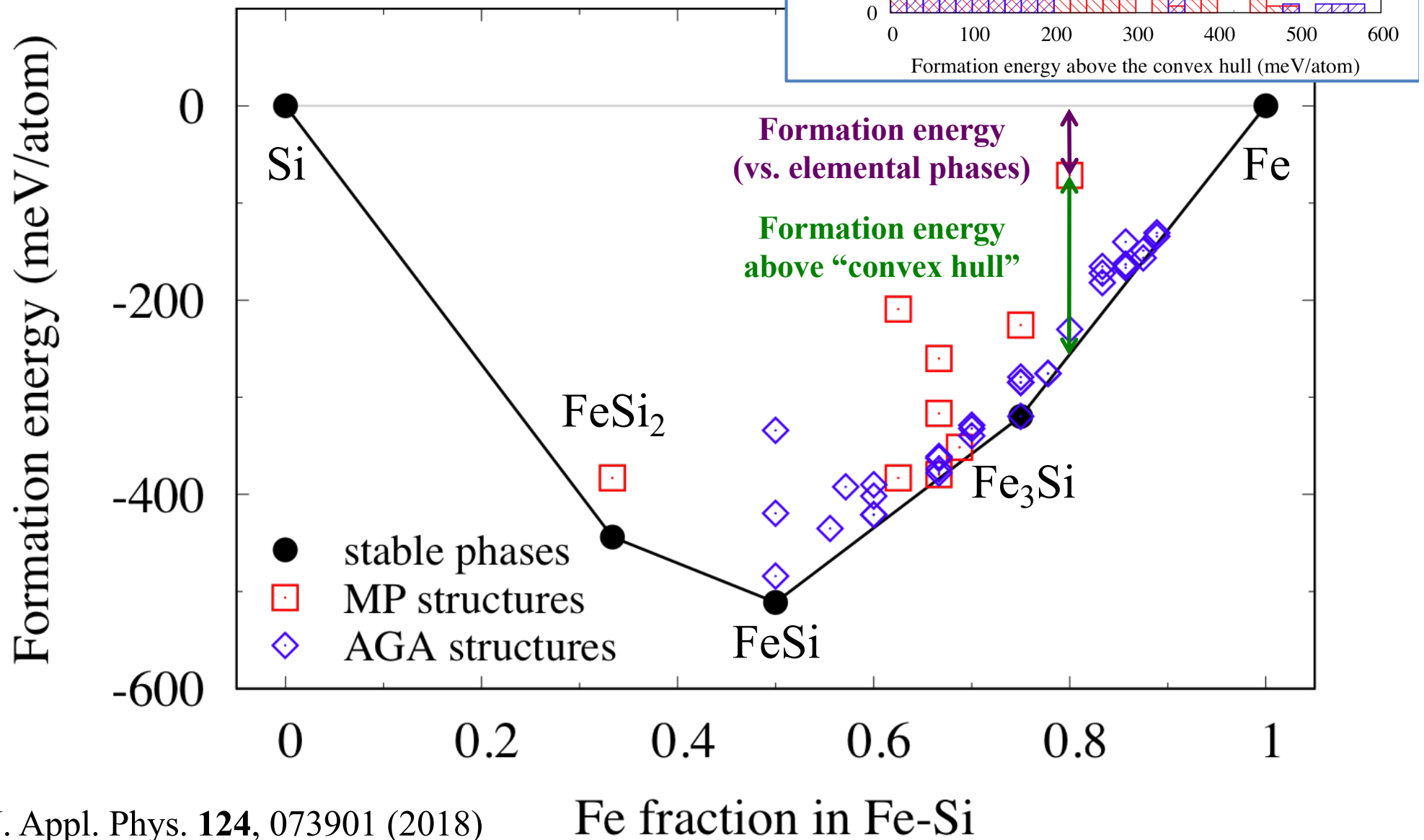
Site-specific data:

magmom: 2.2628 (on-site)

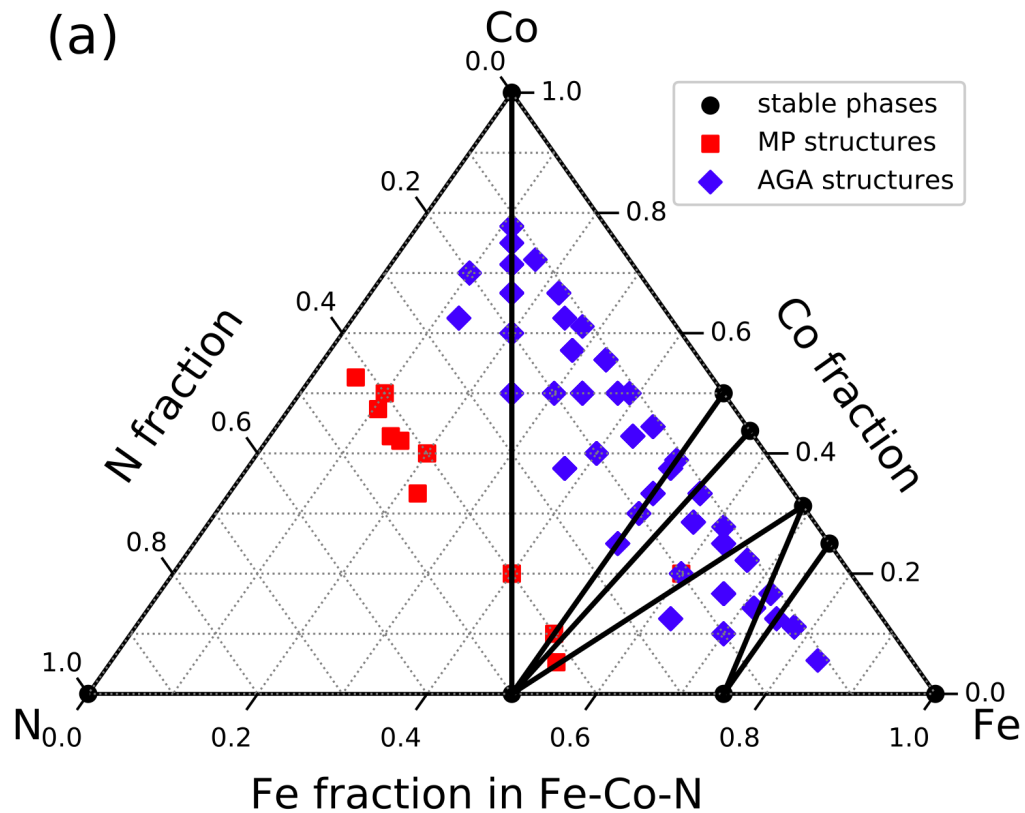
soc: null (on-site)

jij: [null, null] (pairwise)

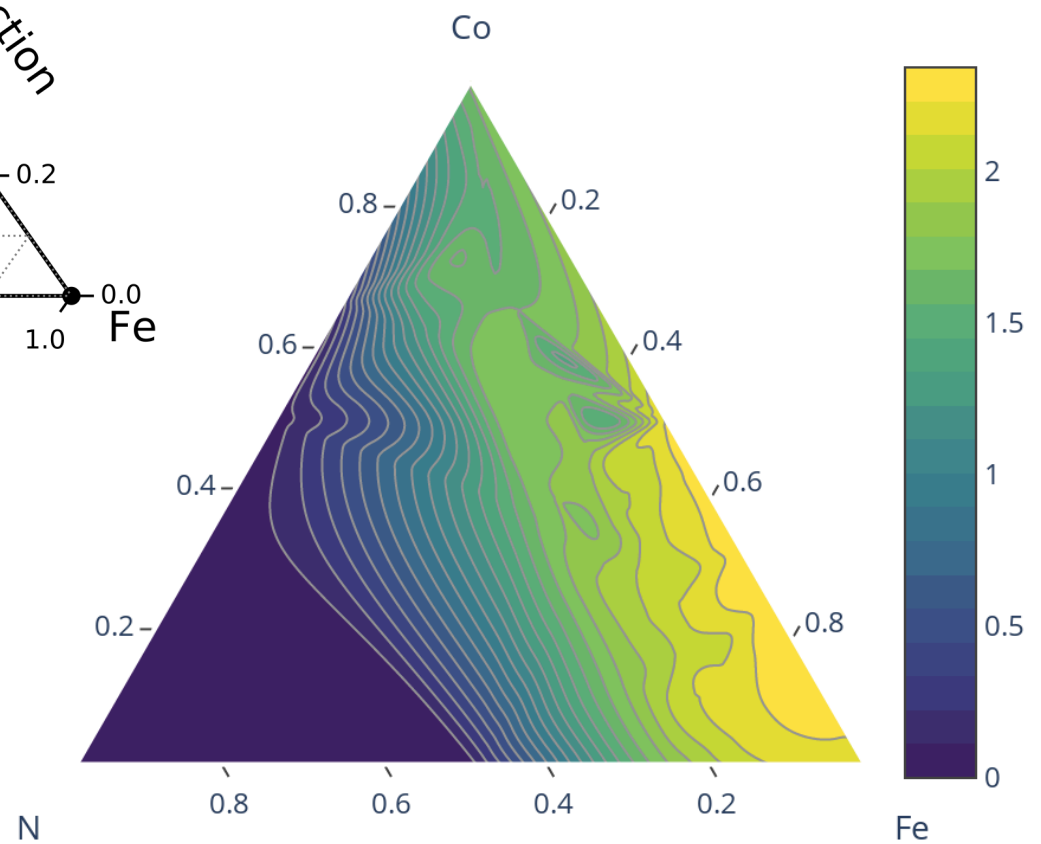
# Metastable structures from AGA search



# Metastable structures from AGA search



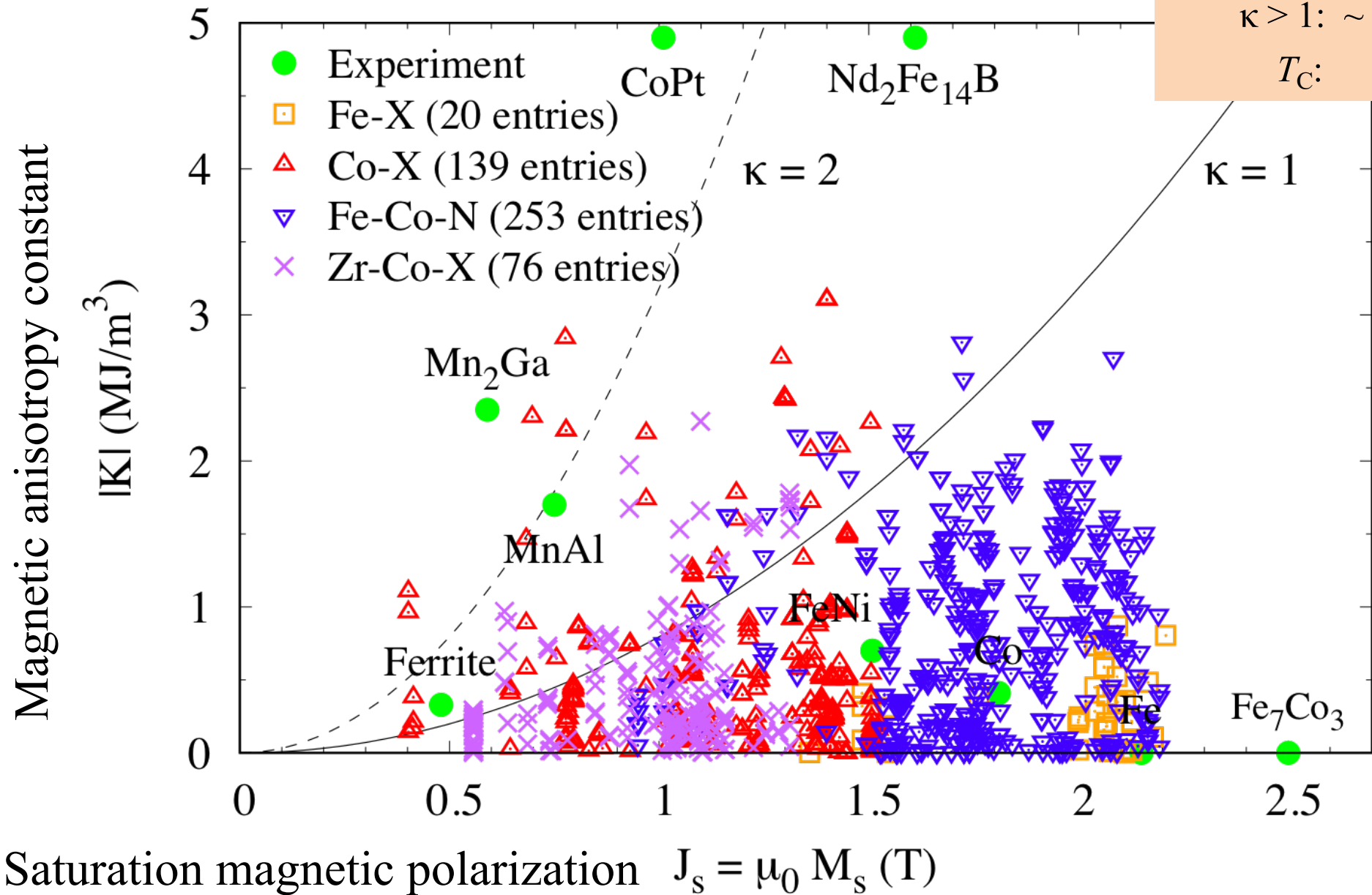
Saturation magnetic polarization  $J_s$





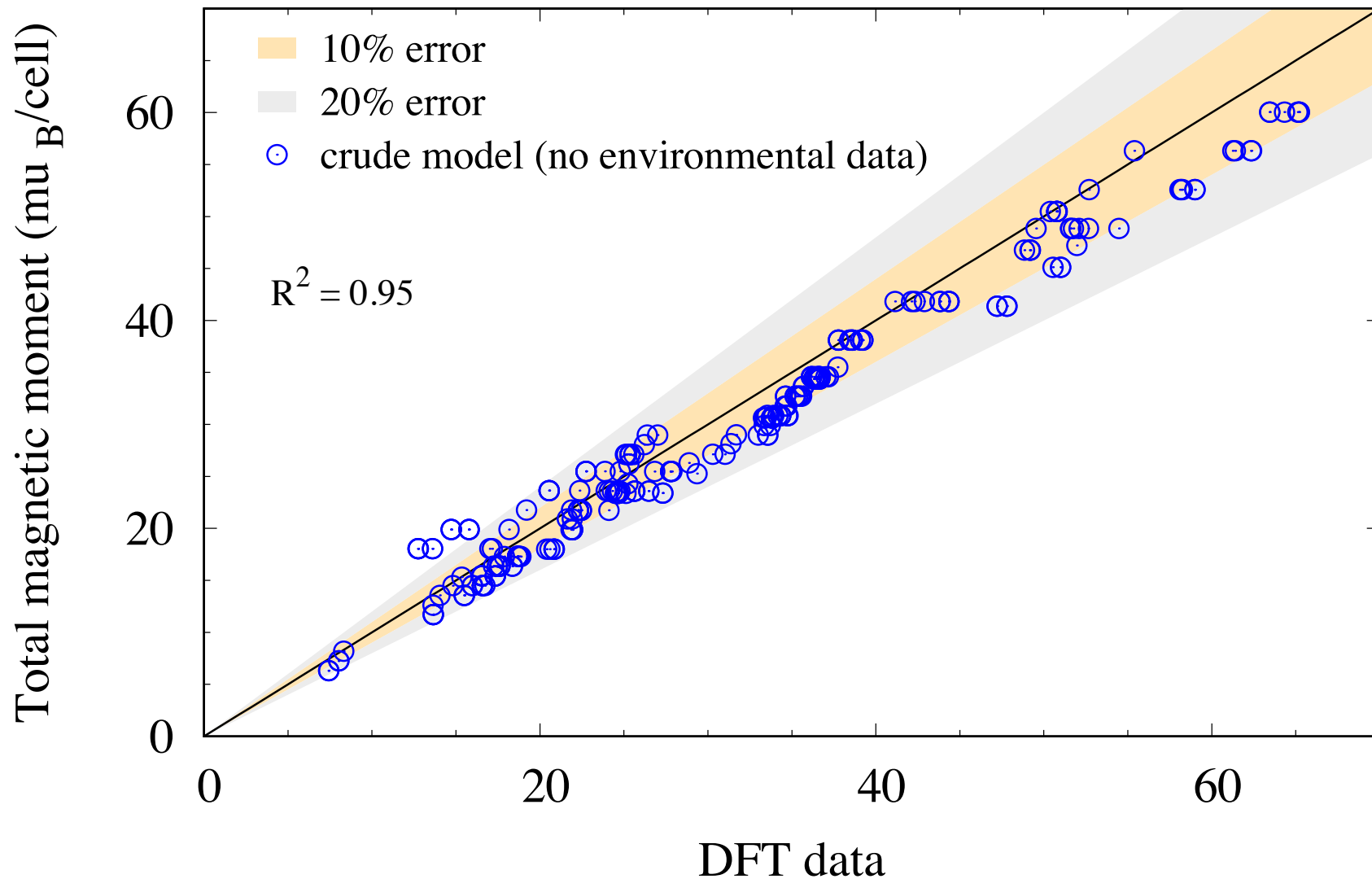
# Magnetic properties of AGA structures

Total: 351 entries  
 $K > 1$ : ~ 33%  
 $\kappa > 1$ : ~ 10%  
 $T_C$ : ?



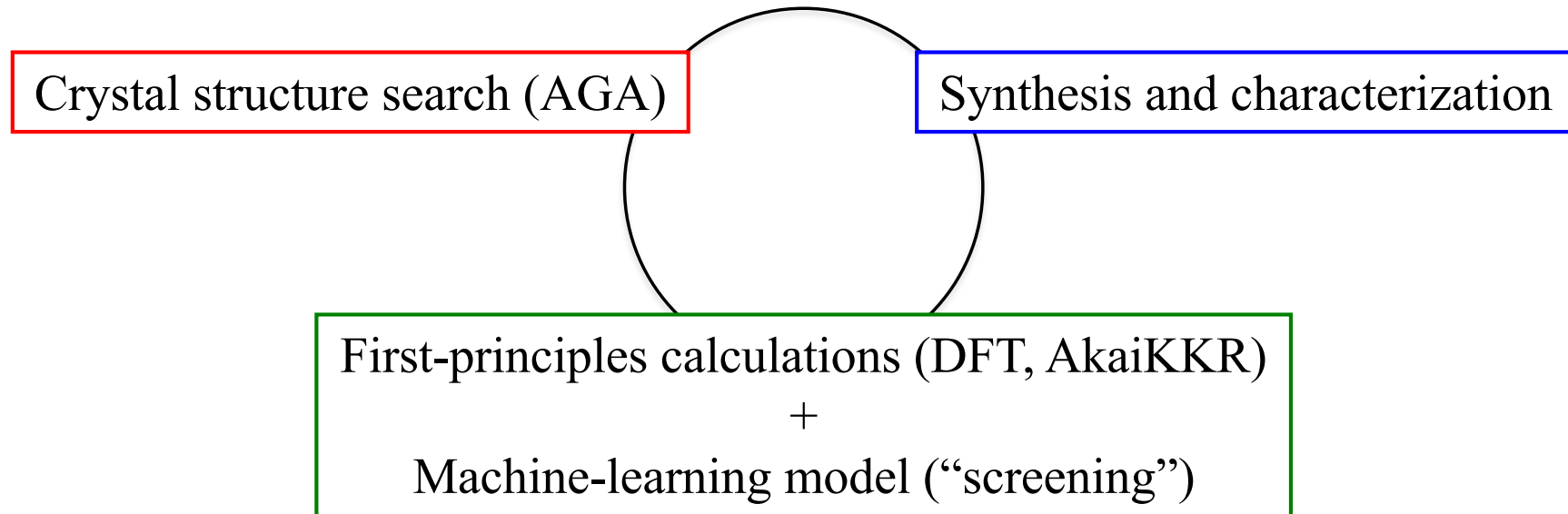
# “Prediction” from site-specific data

Fe-Co-N (259 structures)



# Data-driven approaches for new magnets

---



Targets:

- (i) Nd–Fe–B, Sm–Fe–N
- (ii) rare-earth-lean
- (iii) rare-earth-free: Fe–Co–X, Fe–Mn–X, ...

Concerns:

- f*-electron
- poor properties?
- massive calculations?