

# HΦ講習会－全国共同利用大規模並列計算システムOCTOPUSを用いたハンズオン

## 並列化性能の紹介

2019/10/16 Wed.  
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- 01 Project for advancement of software usability in materials science
- 02 Parallelization by vector division
- 03 Parallelization for full diagonalization

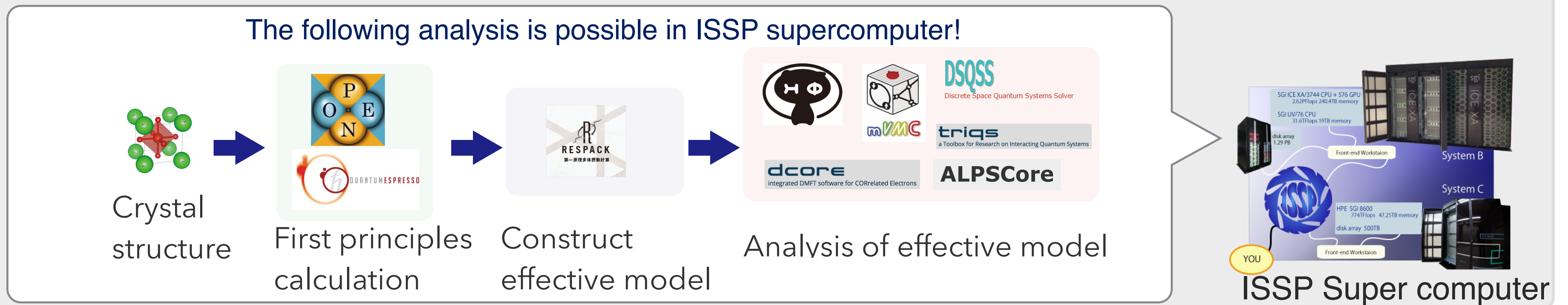
# Project for advancement of software usability in materials science

To create an easy-to-use supercomputer environment by improving the usability of key software in condensed matter physics.



Upgrade 2 software per year with the following team (Workload: 5 man months per software)

- ☆ Coordinator ISSP staff ( 1 staff per project)
- ☆ Project manager (sometimes developer) Kazuyoshi Yoshimi
- ☆ Main developer Yuichi Motoyama



# Building communities through supercomputer/projects

ex. Cooperation with mathematical library  $K\omega$  and  $H\Phi$



What is  $K\omega$  ?



## $K\omega$

Openness:3 ★★★ Document quality:1 ★★★

$K\omega$  implements large-scale parallel computing of the shifted Krylov subspace method. Using  $K\omega$ , dynamical correlation functions can be efficiently calculated. This application includes a mini-application for calculating dynamical correlation functions of quantum lattice models such as the Hubbard model, the Kondo model, and the Heisenberg model in combination with the quantum lattice solver of quantum many-body problems,  $H\Phi$ .

ref. <https://ma.issp.u-tokyo.ac.jp/en/app/546>

It is possible to directly examine the properties of matrix vectors by outputting them from  $H\Phi$ .  
→ Solve new problems in large matrices in cooperation with mathematical researchers.

# Parallelization (1)

## Parallelization by vector division of Hilbert space (MPI)

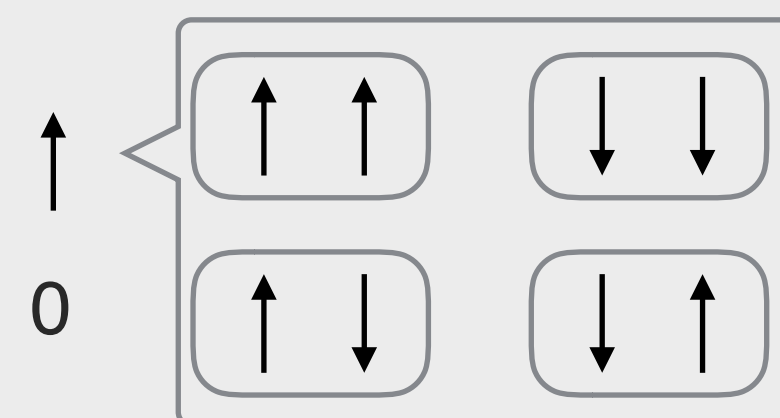


MPI parallelization: The number of processes applied to the subspace of Hilbert space  
Thread parallelization: Hamiltonian vector product part using OpenMP

Ex.) MPI parallelization : Spin system (L=3, using 2 processes)

Rank 0: up spin

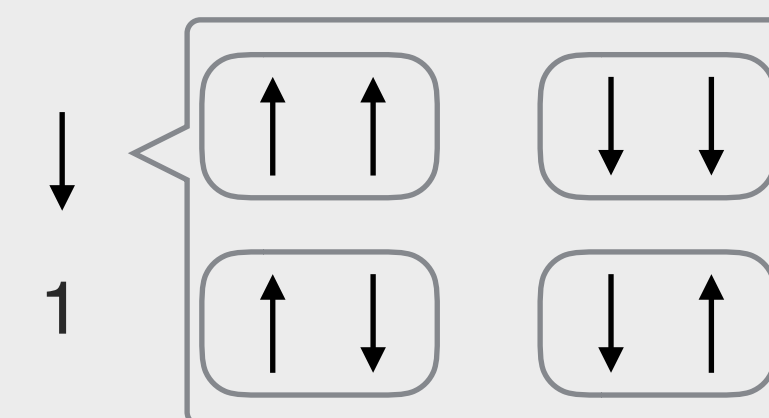
Inner process



0~3

Rank 1: down spin

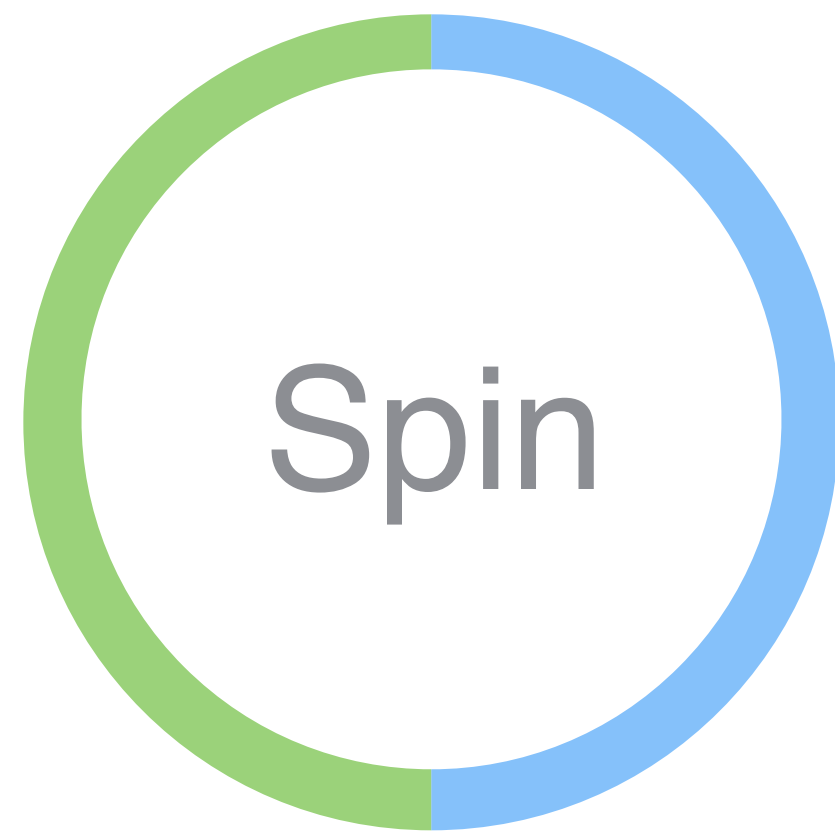
Inner process



0~3



# How to parallelize with HΦ: Number of processes required for parallelization



↑, ↓



2 states per site  
Process number :  $2^N$



0, ↑, ↓, ↑↓



4 states per site  
Process number :  $4^N$



0, ↑, ↓, ↑↓



4 states per site (For spin,  
0, ↑ ↓ states are excluded)  
Process number :  $4^N$

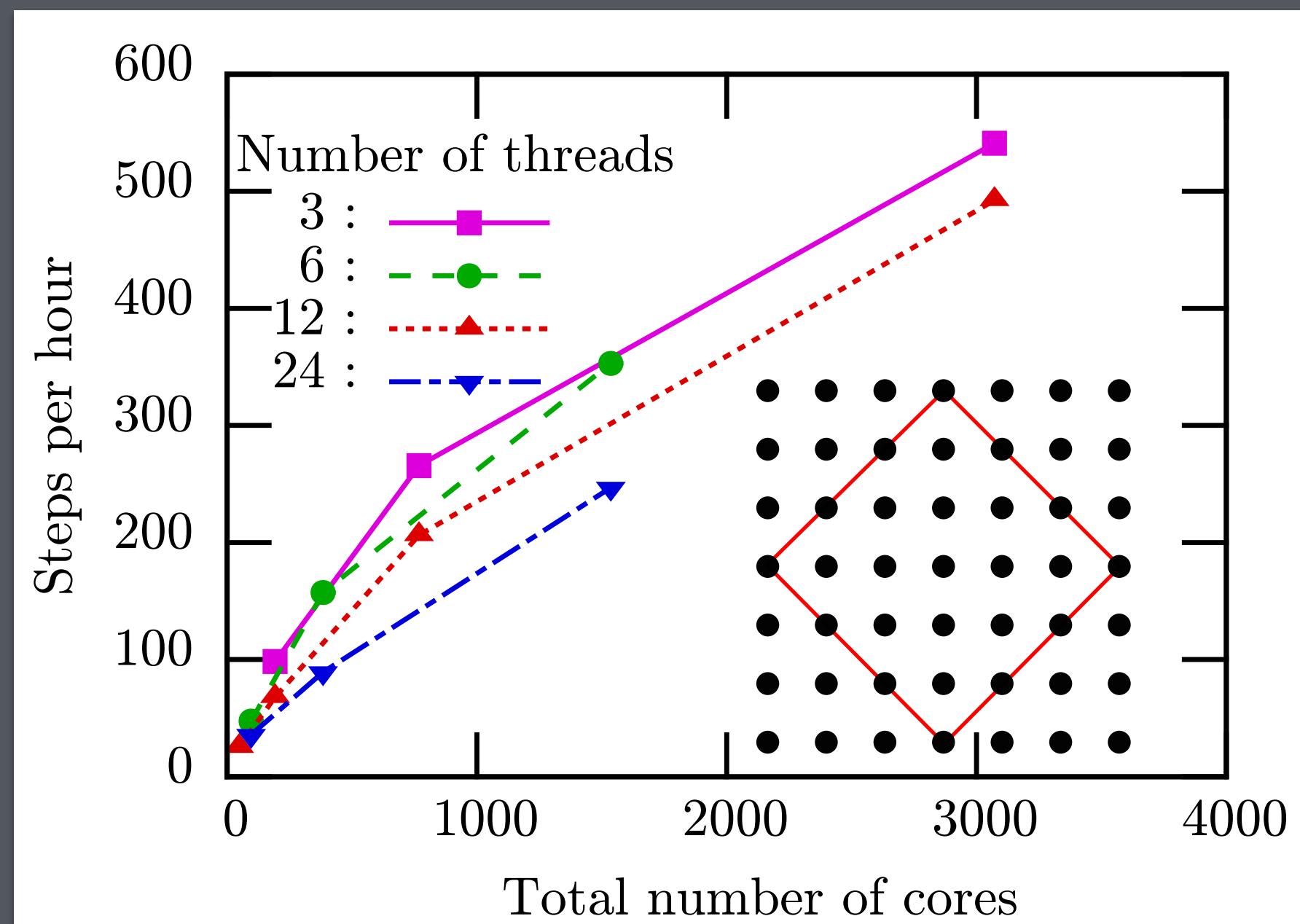
# Benchmark result (1)

## Parallelization by vector division of Hilbert space



18 site Hubbard model (half-filling,  $2S_z=0$ ,  $U/t = 8$ )  
ISSP super computer system B

- The number of steps increases with increasing the number of cores.
- Basically, flat MPI tends to be faster.



Total number of cores dependence of TPQ steps per hour

# Parallelization (2)

## Parallelization of full diagonalization

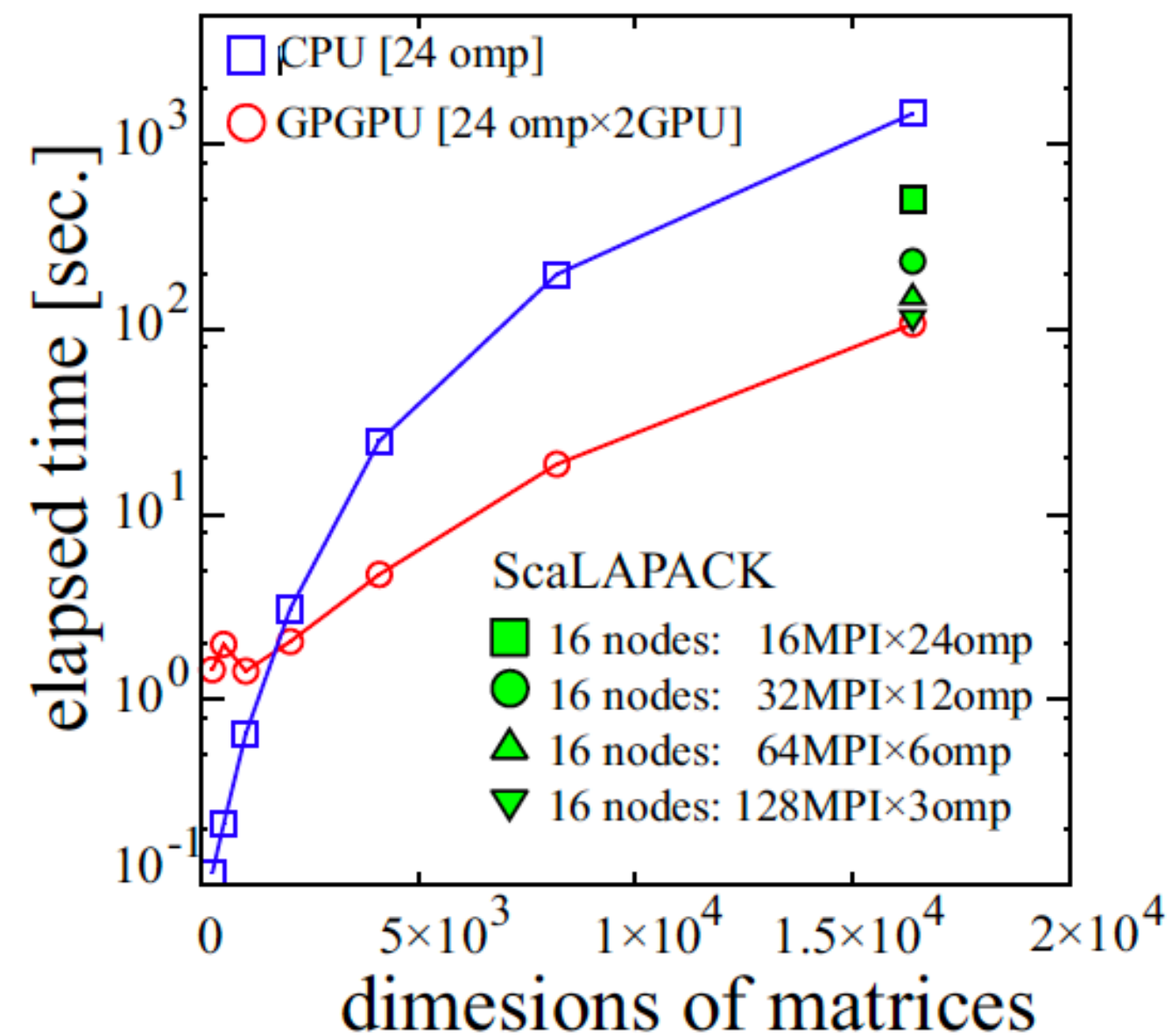


First, Hamiltonian matrix is calculated by single process.  
Then, then matrix is diagonalized by the following library

1. LAPACK (single process)
2. ScaLAPACK (using MPI)
3. MAGMA (using GPU)

## Benchmark result (2)

~ Full diagonalization  
using ScaLAPACK and MAGMA



The dimensions of matrices and the elapsed time for full diagonalization

- System: ISSP Super computer systemB ACC node
  - CPU: Intel Xeon 2.5 GHz (12cores) x2
  - GPU: Nvidia Tesla K40 x 2
- ScaLAPACK: Faster with more processes.
- MAGMA works well if the matrix size is larger than 10<sup>3</sup>.

ref. ) "Implementation of GPGPU computing in full diagonalization for HΦ", T. Misawa and K. Yoshimi, Activity report 2017/Supercomputer Center, Institute for Solid State Physics, The University of Tokyo, 305-307 (2017).